

# Similar Part Rearrangement With Pebble Graphs



Athanasios Krontiris, Rahul Shome, Andrew Dobson, Andrew Kimmel and  
Kostas E. Bekris  
Department of Computer Science  
Rutgers University



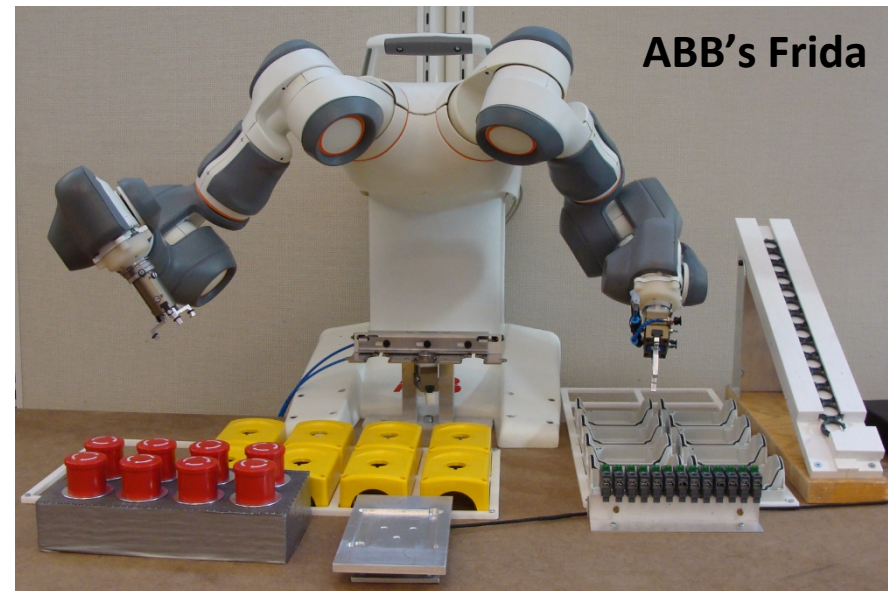
*Warehouse management*



*Cluttered manipulation*



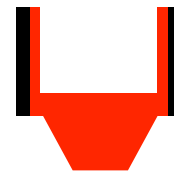
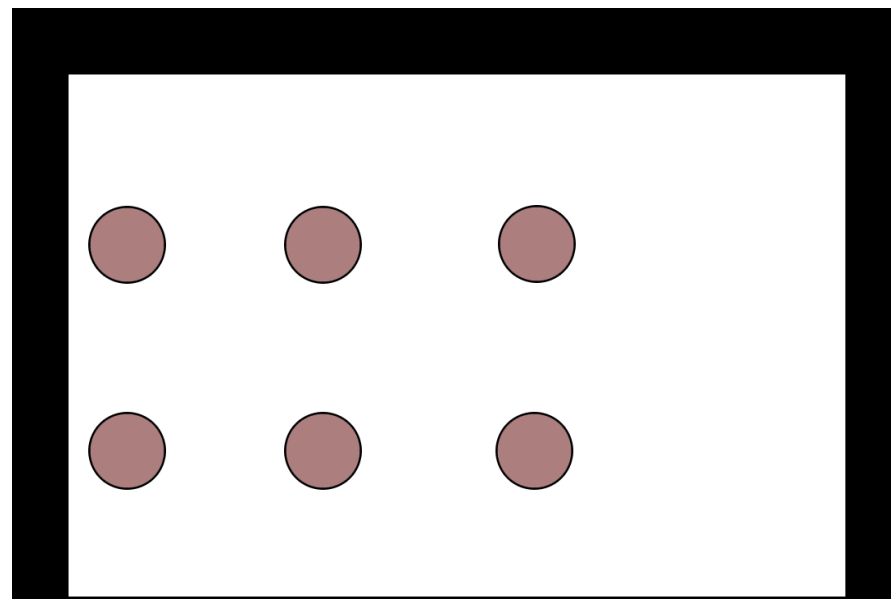
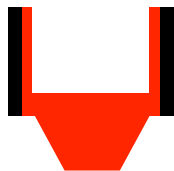
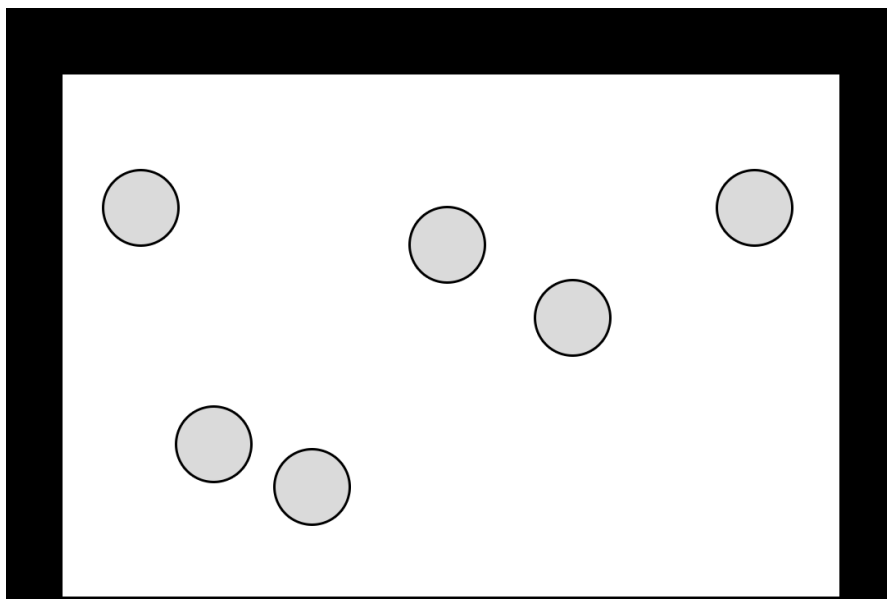
- Humanoid/compliant robots become available for industrial applications
- They need to operate in less structured, cluttered, narrow workspaces where reaching every object is not easy
- One capability that is needed:
  - Rearrange products or components in a desired way



# Unlabeled Rearrangement Problem

Given an initial and a final object arrangement compute a continuous manipulation path to move the objects from the initial to the final arrangement without collisions.

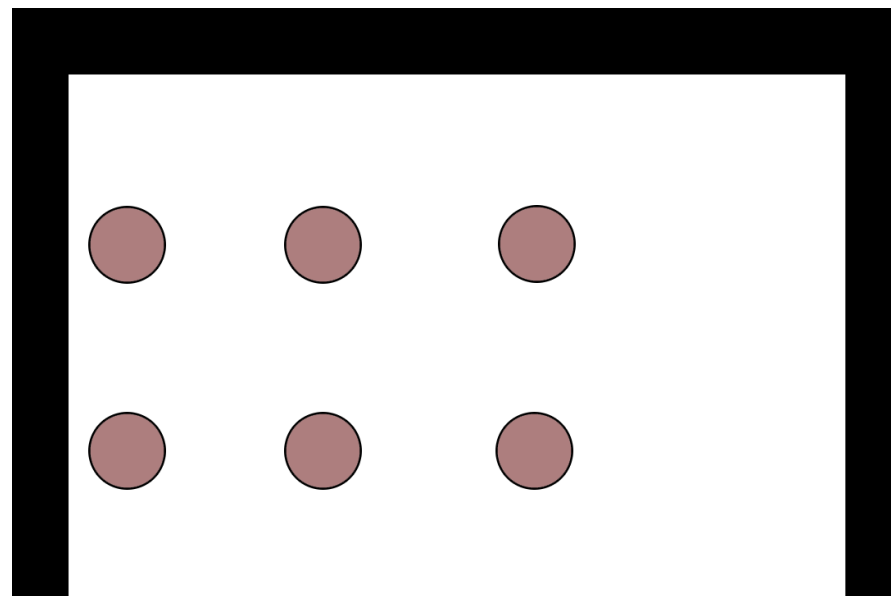
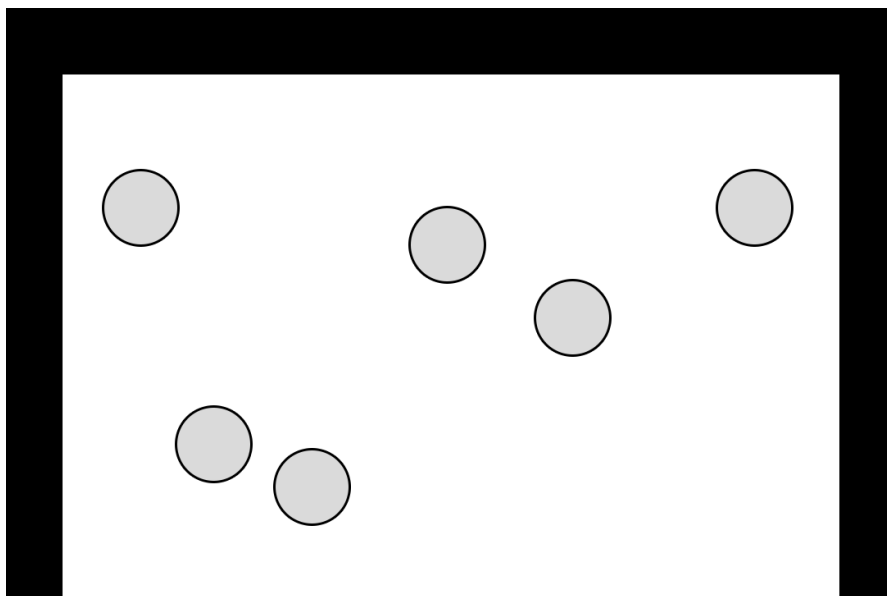
- Focus on motion planning and combinatorial aspects



- High-dimensional challenge
  - 7 DOF arms + 6 DOF per object
- Brings together many other problems:
  - Manipulation and grasping
  - Multi-robot motion planning

Easy instances:  
Monotone Challenges

Hard instances:  
Non-Monotone  
(an object must be  
grasped more than once)



• Planning among movable obstacles & Manipulation

- Navigation Among Movable Obstacles.

[J. van den Berg, M. Stilman et al, 2008]

- Manipulation Among Movable Obstacles.

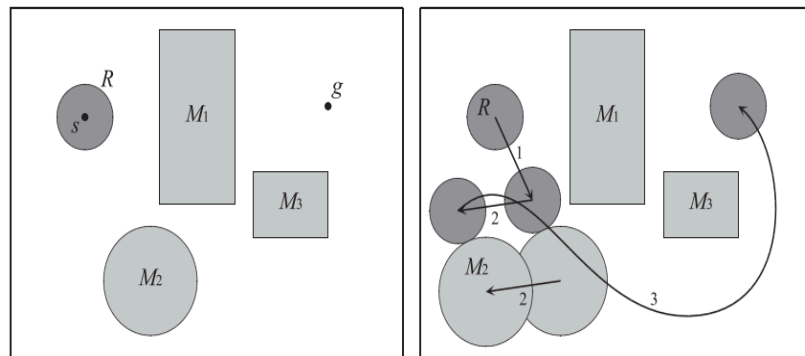
[M. Stilman et al, 2007]

- Minimum Constraint Displacement.

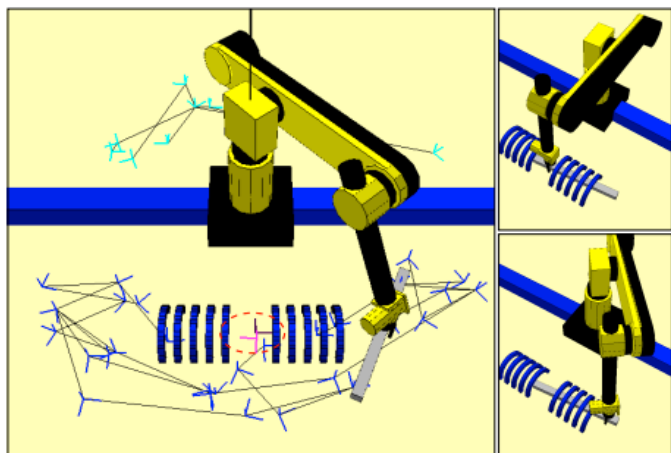
[K. Hauser, 2012]

- Manipulation Planning with Probabilistic Roadmaps.

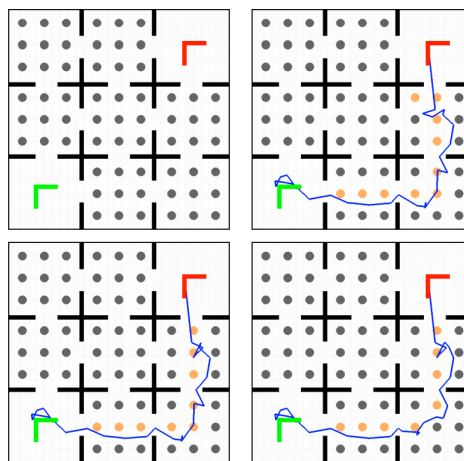
[T. Simeon, J.-P. Laumond, et al., 2004]



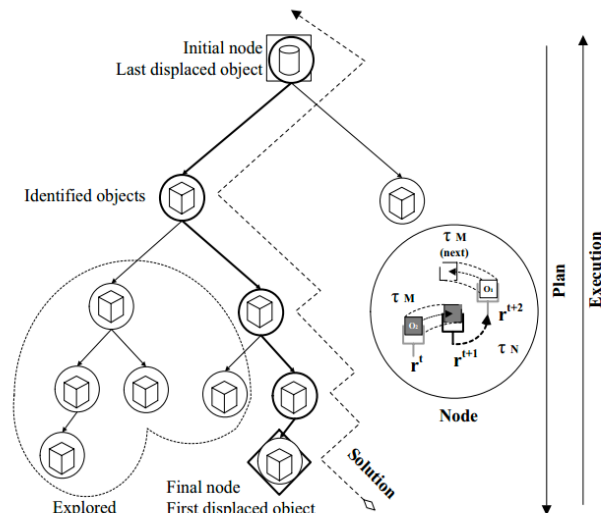
[J. van den Berg, M. Stilman et al, 2008]



[T. Simeon, J.-P. Laumond, et al., 2004]



[K. Hauser, 2012]



[M. Stilman et al, 2007]

Rearrangement planning is a prototypical example of

- integrating task and motion planning
- combining continuous and discrete reasoning
- Motion planning:
  - The continuous motions for reaching to and grasping motions
- Task planning:
  - Placing objects to different locations (combinatorial aspect)

Idea:

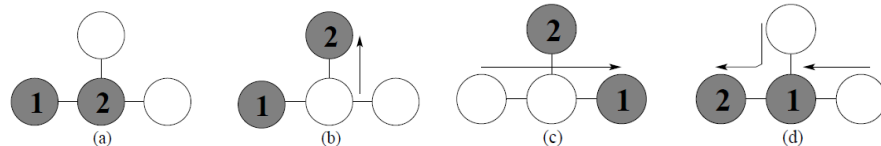
- Implicitly represent entire sets of states in a compact manner without the need to enumerate them
- Use multi-robot path planning tools in this direction

- Multi-robot planning.

- Discrete solvers for multi-robot motion planning.

[Luna, R., Bekris, K.E., 2011]

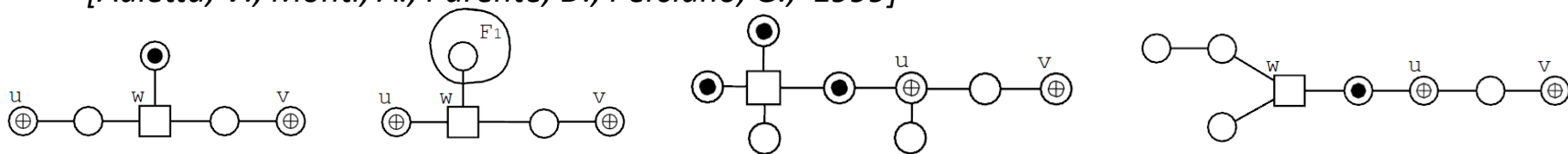
[Yu, J., LaValle, S.M., 2012]



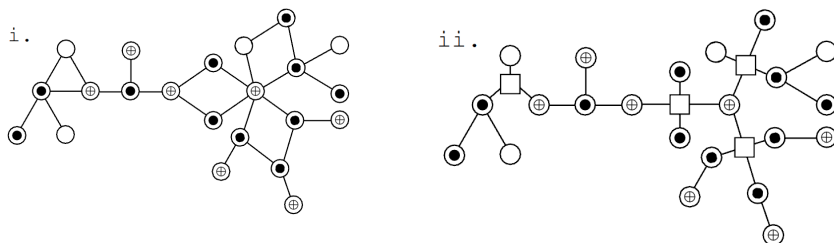
[Luna, R., Bekris, K.E., 2011]

- Feasibility test for pebble motion on graphs.

[Auletta, V., Monti, A., Parente, D., Persiano, G., 1999]

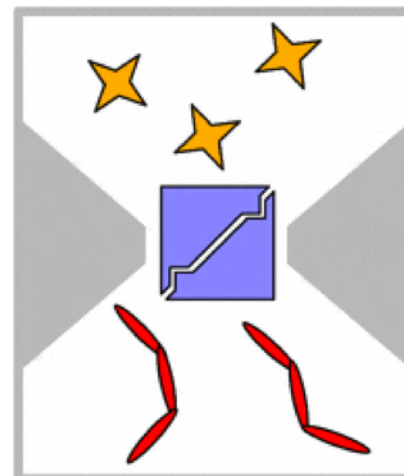


[Goraly, G., Hassin, R., 2010]



- Continuous multi-robot motion planning.

[Solovey, K., Halperin, D. 2012]

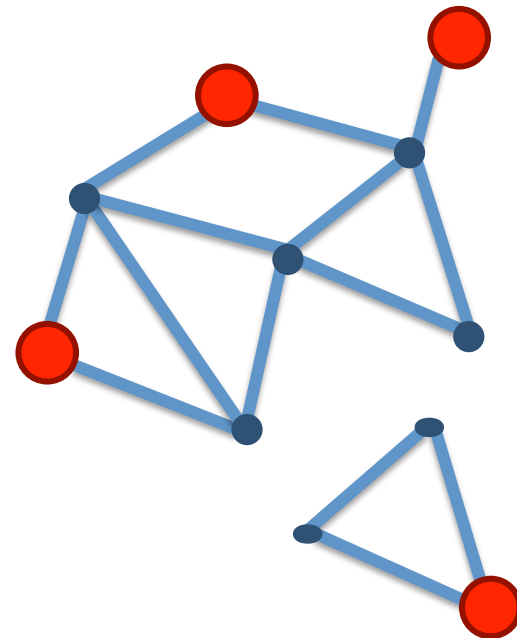


[Solovey, K., Halperin, D. 2012]



# Approach

- Given a graph with multiple connected components
- And  $k$  unlabeled pebbles that can occupy vertices
- A set of reachable arrangements can be represented compactly by:
  - the graph
  - and a “signature” indicating the number of pebbles on each connected component

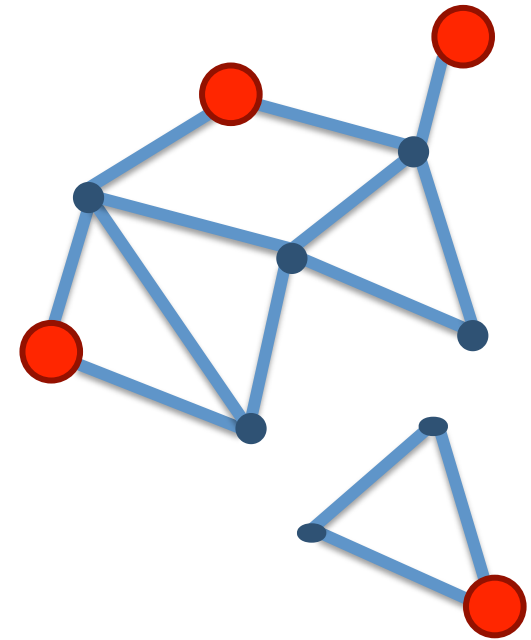


$K = 4$   
Signature =  $\{3, 1\}$

---

Linear time to find a path between any two reachable arrangements

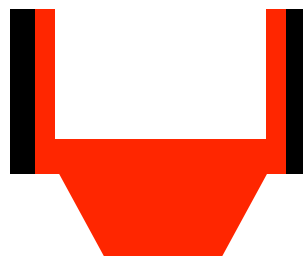
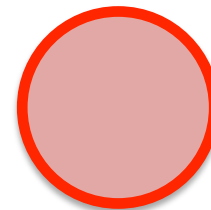
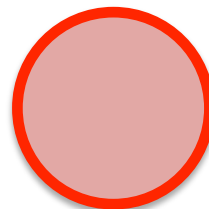
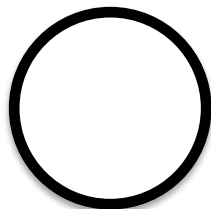
- Difference between discrete abstraction and manipulation challenge:
  - Requires no collisions between objects occupying two nodes and between nodes/edges
  - The manipulator must be able to move objects along edges
- Approach: Try to abstract out the motion of the manipulator and reason directly about the movement of objects

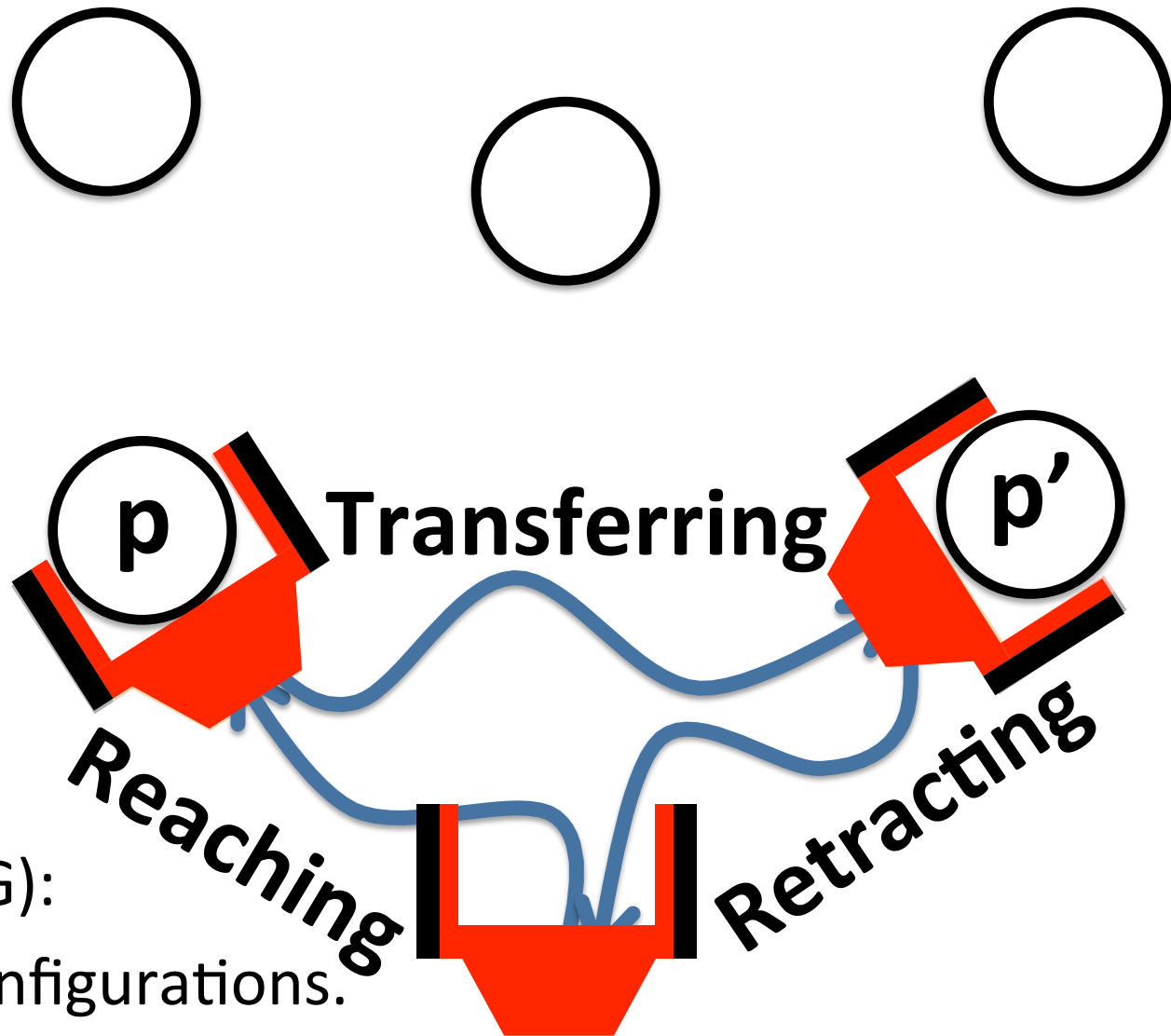


$K = 4$

Signature = {3,1}

- Given a safe configuration for the robot.
- Given initial arrangement.
- And the target arrangement.





- Rearrangement

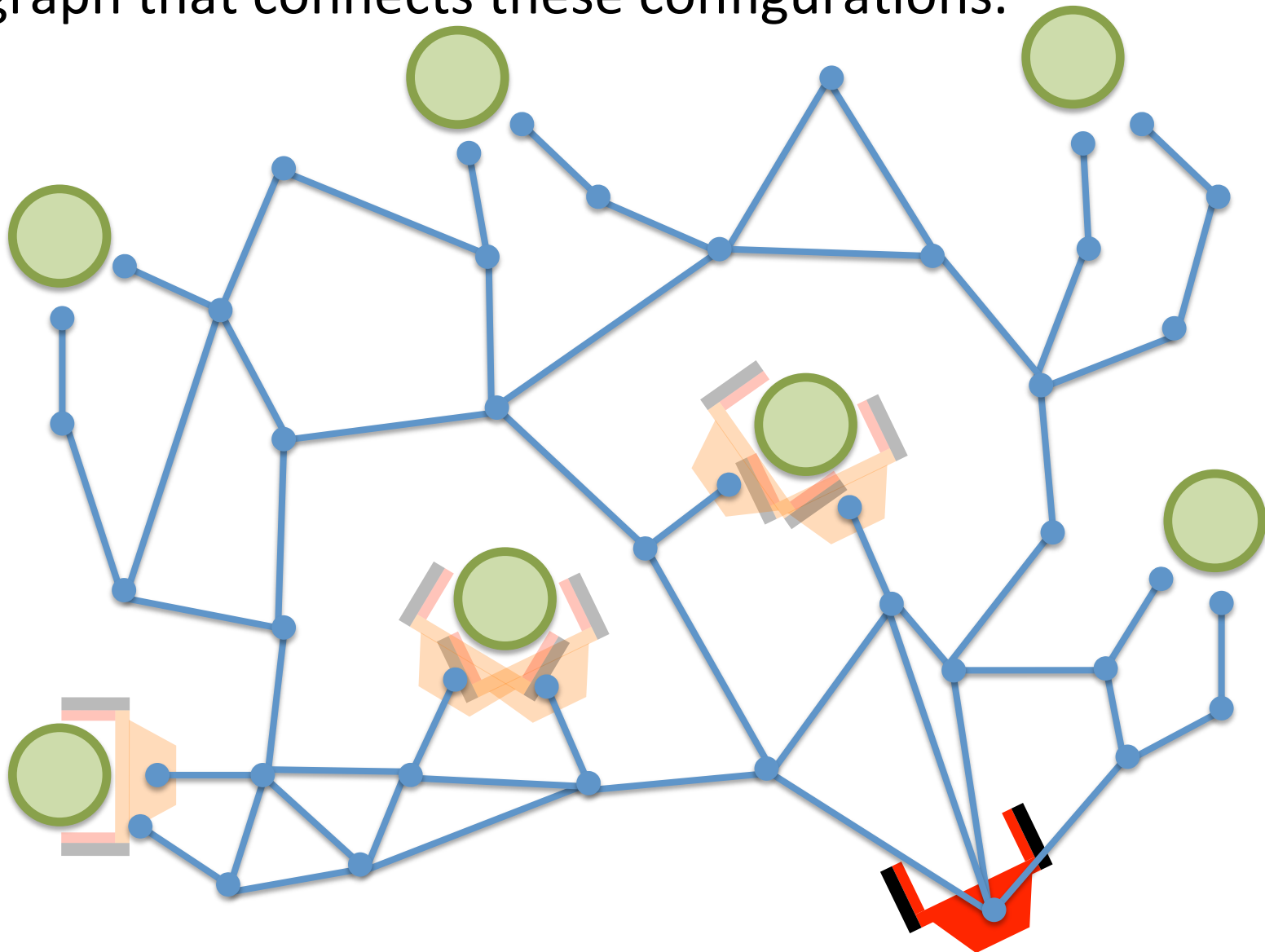
Pebble Graph (RPG):

- Nodes: Stable configurations.

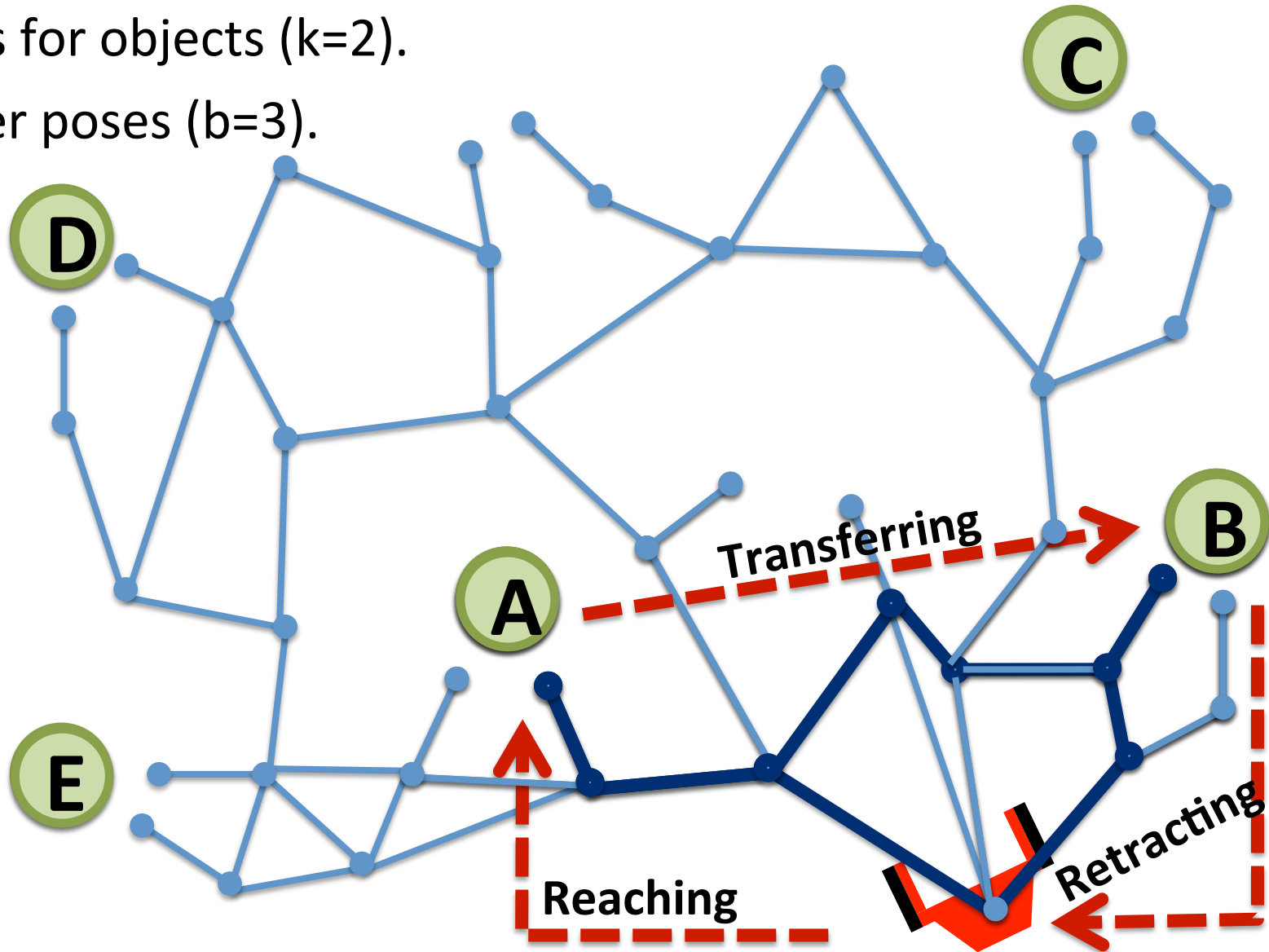
- Edges: Collision free motions of the arm that transfer an object between poses.



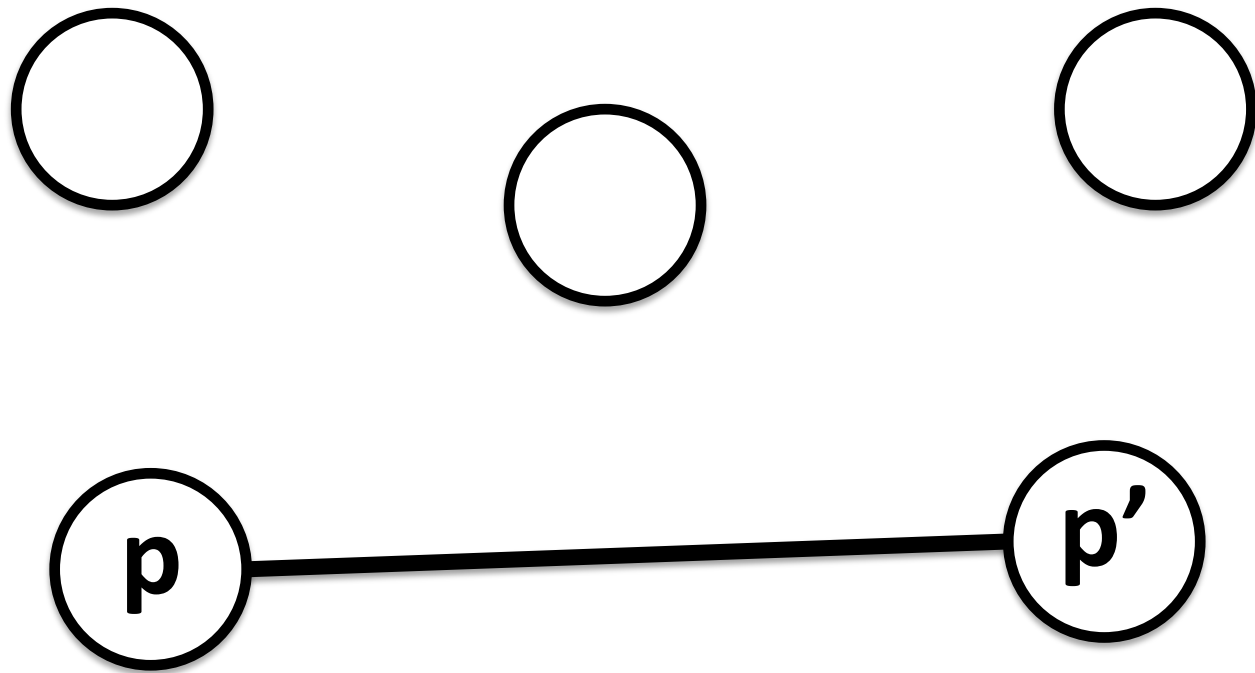
- Build a graph that connects these configurations.



- Select  $k+b$  poses.
  - $k$  poses for objects ( $k=2$ ).
  - $b$  helper poses ( $b=3$ ).





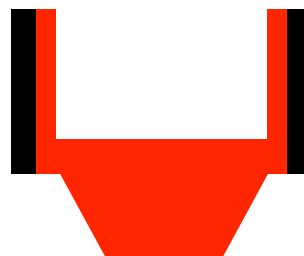


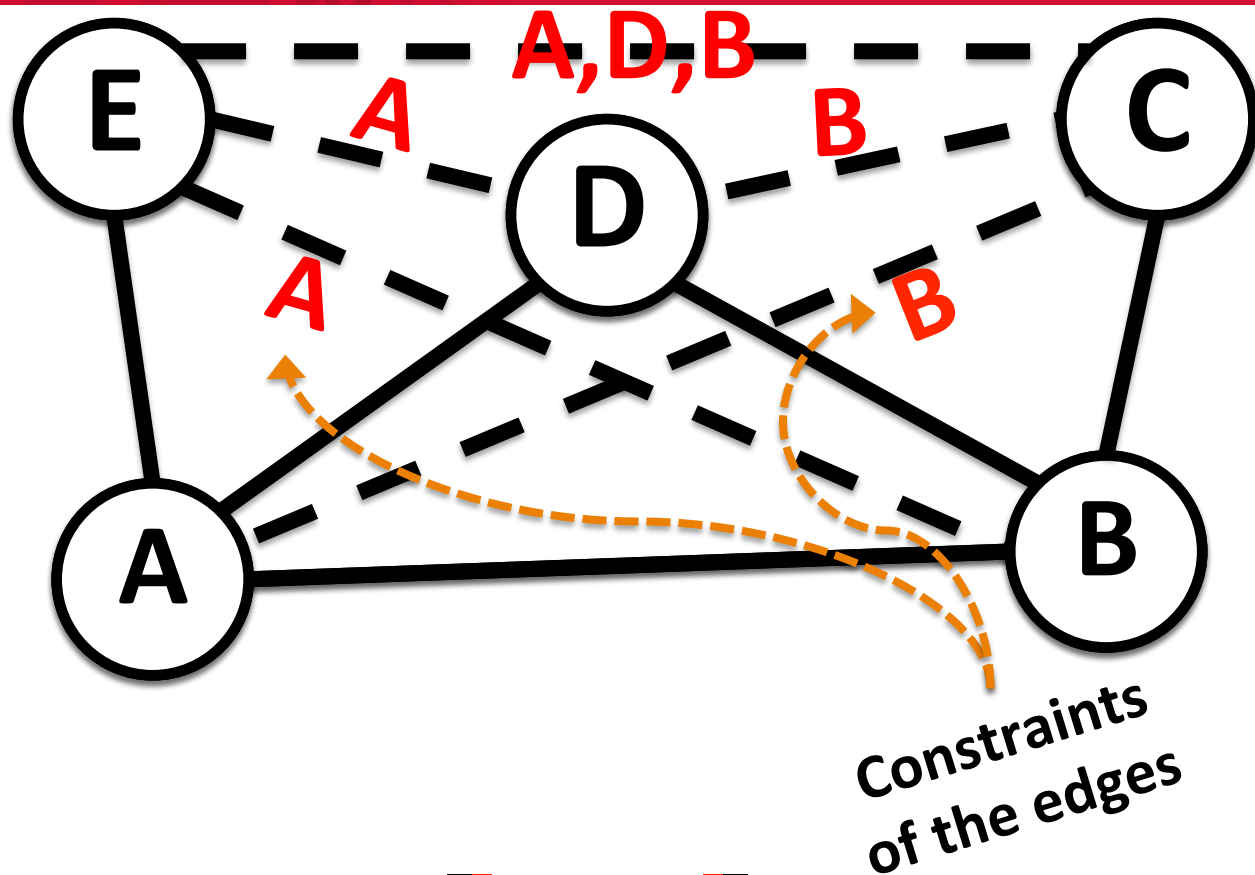
- Rearrangement

Pebble Graph (RPG):

- Nodes: Stable configurations.

- Edges: Collision free motions of the arm that transfer an object between poses.

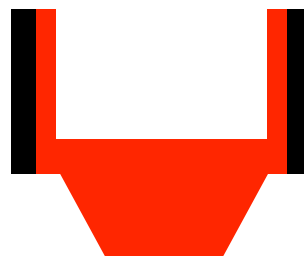




- Rearrangement

Pebble Graph (RPG):

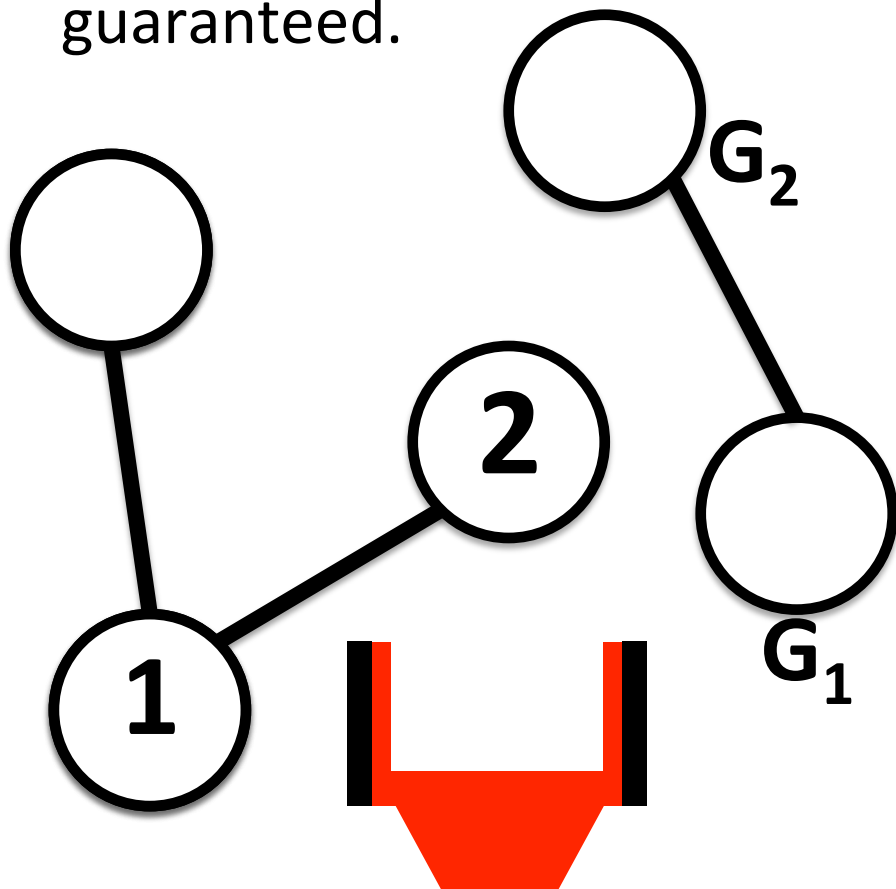
- Nodes: Stable configurations.



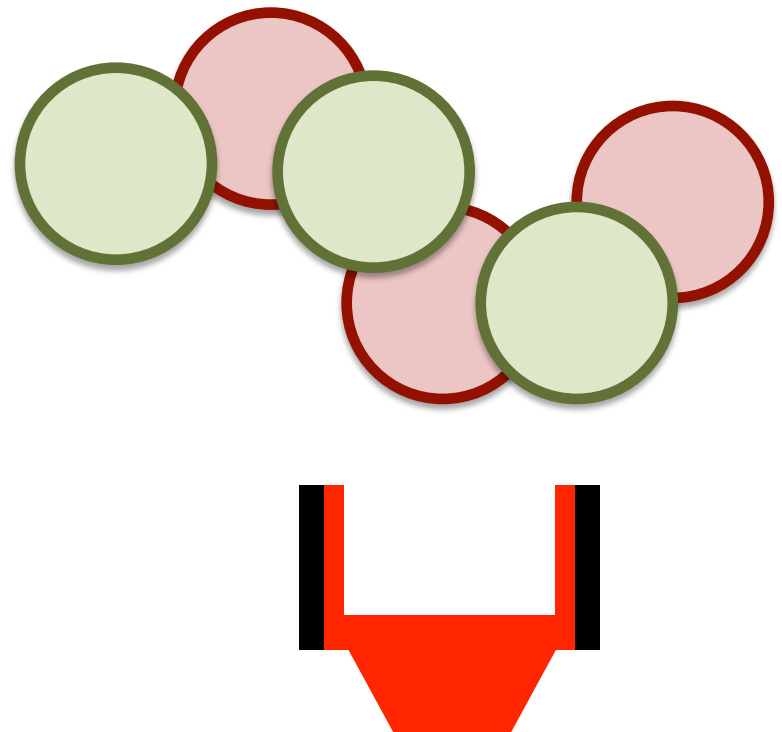
- Edges: Collision-free motions of the arm that transfer an object between poses **regardless of object placements.**

- If initial/target arrangement on same component: Victory!
- A rearrangement may not be solvable with a single RPG

Issue 1: Connectivity is not guaranteed.

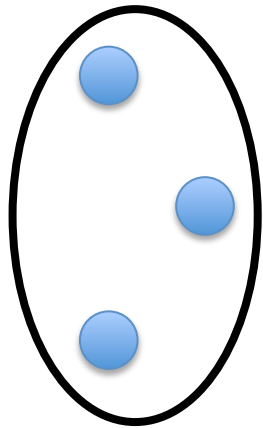


Issue 2: Poses in the initial and target arrangements could be overlapping.

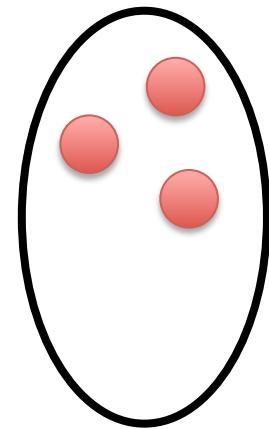
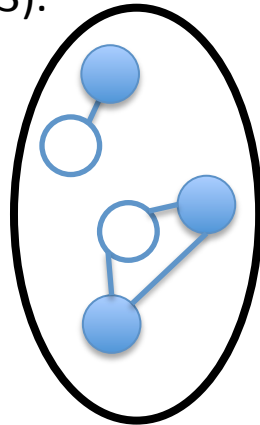




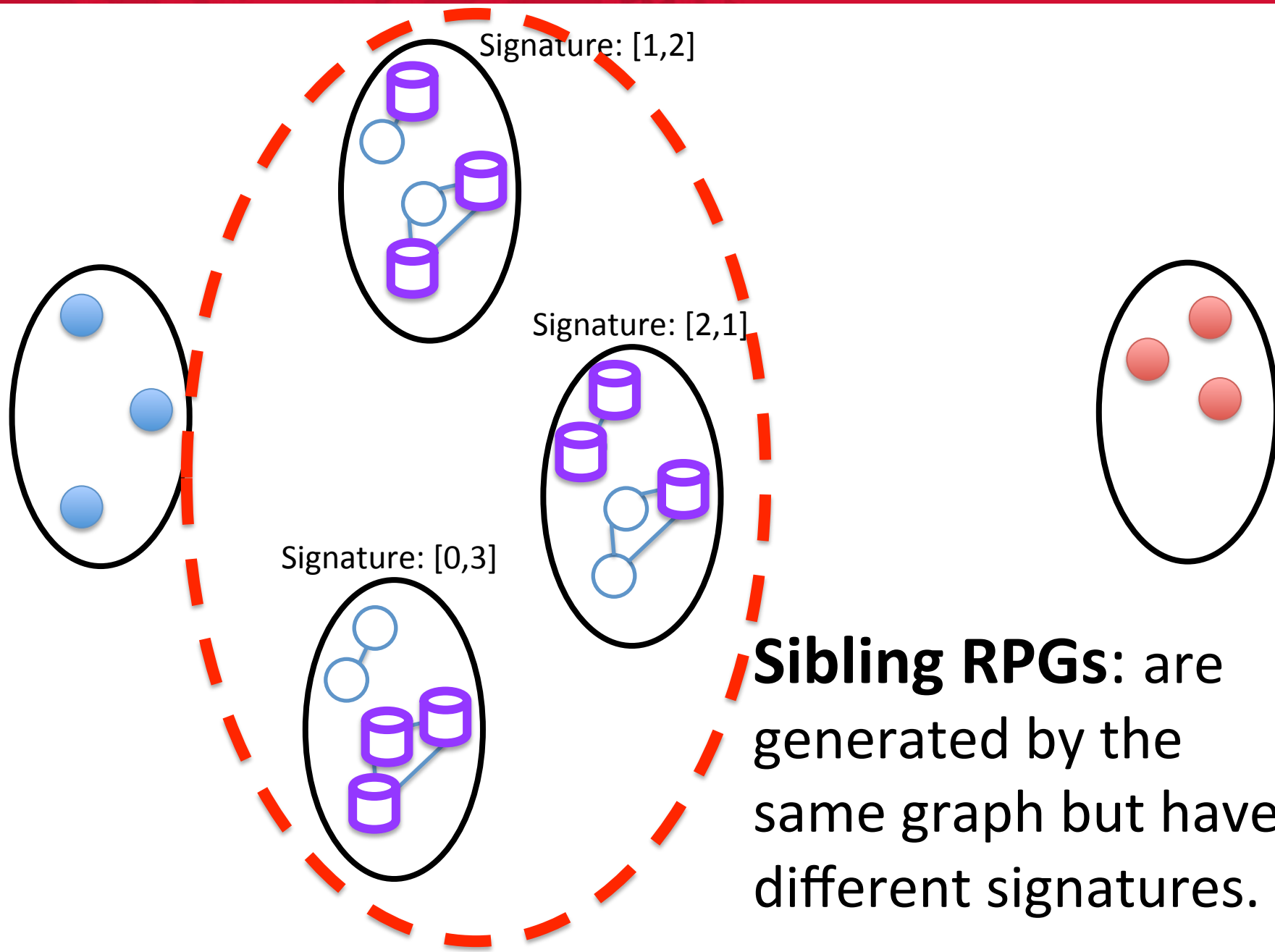
- $k$  poses for objects ( $k=3$ ).
- $b$  helper poses ( $b=2$ ).



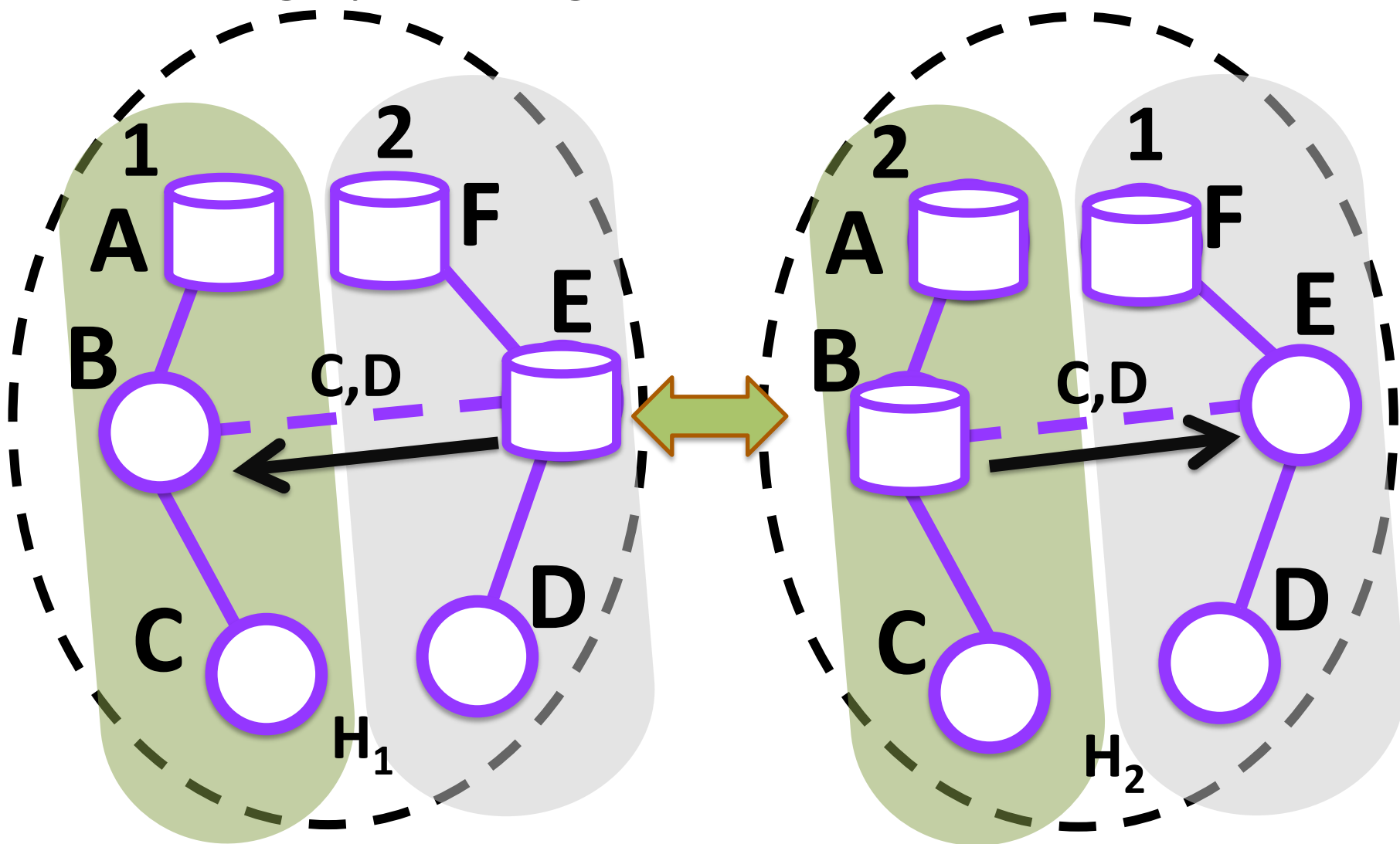
Initial  
arrangement



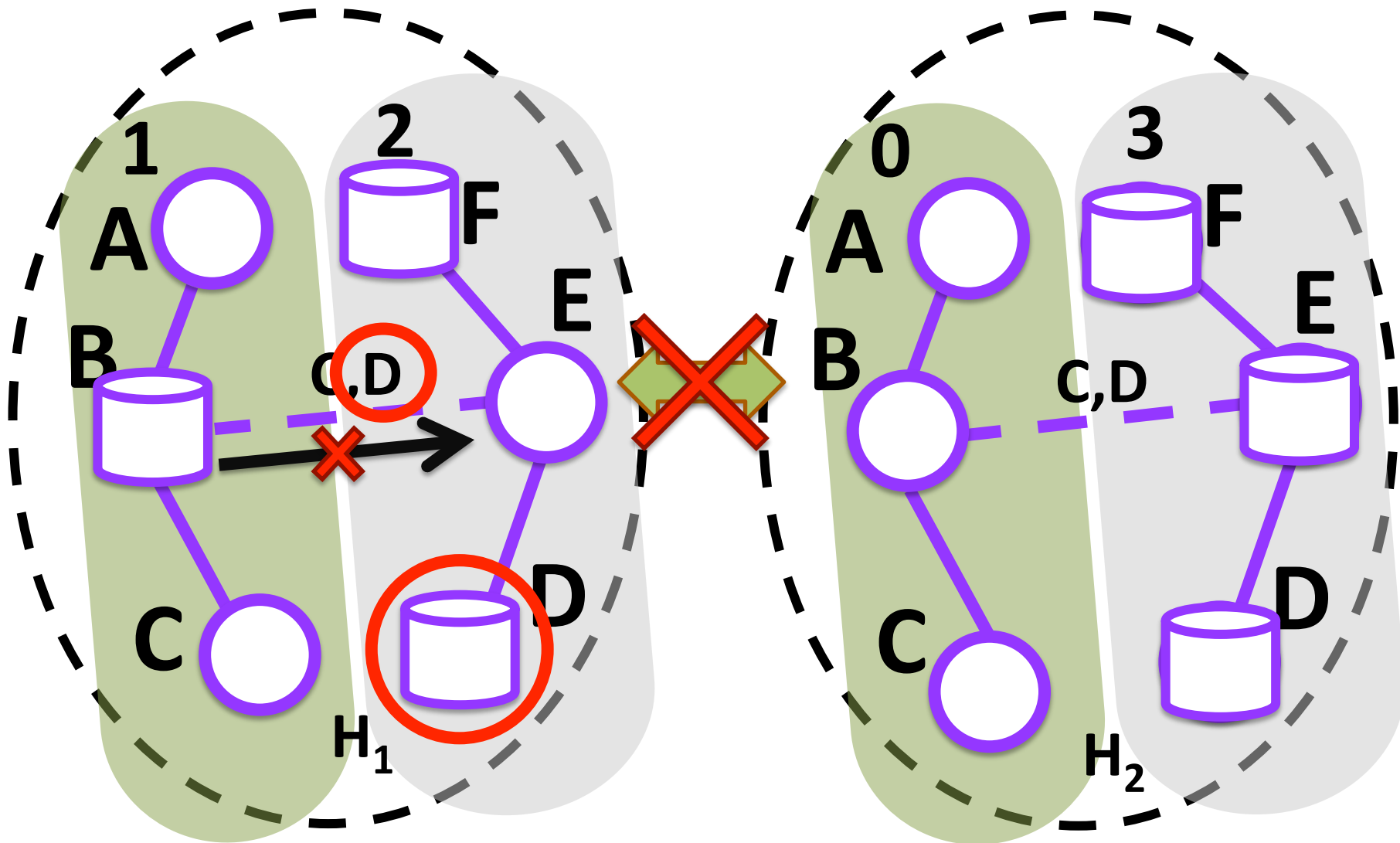
Target  
arrangement



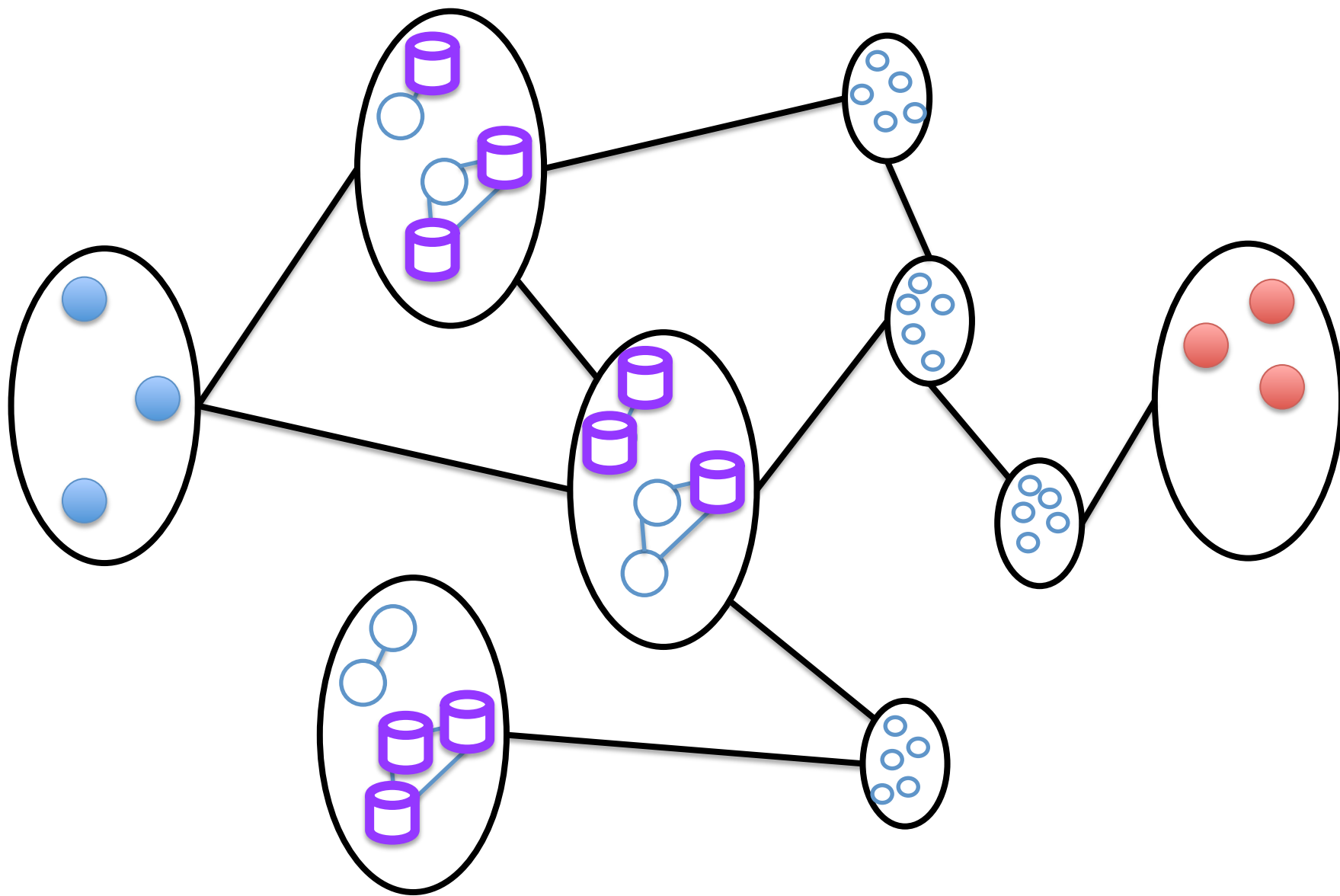
- Use signatures to connect super-nodes corresponding to the same graph (siblings).



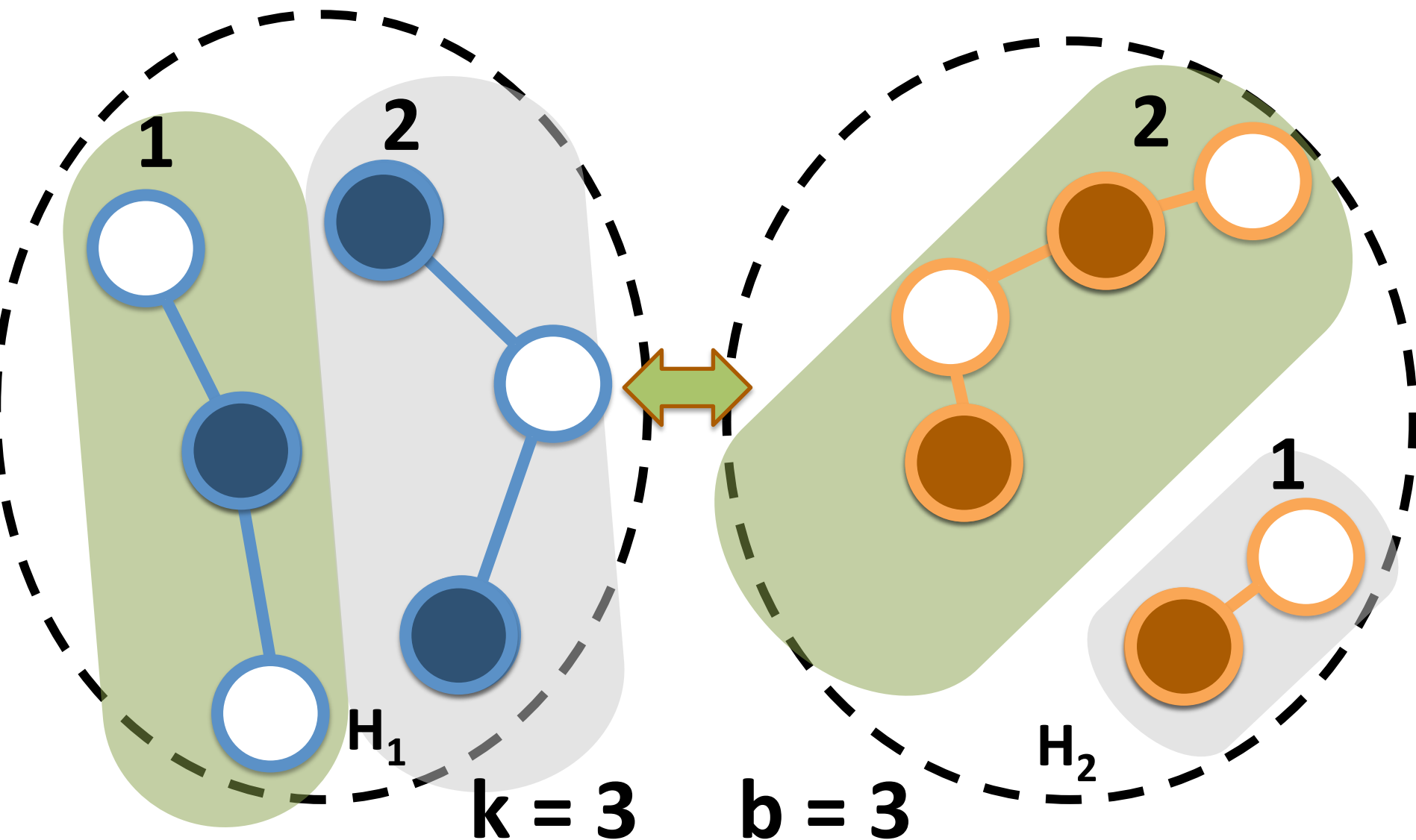
- Siblings that will not be connected because of the signatures.



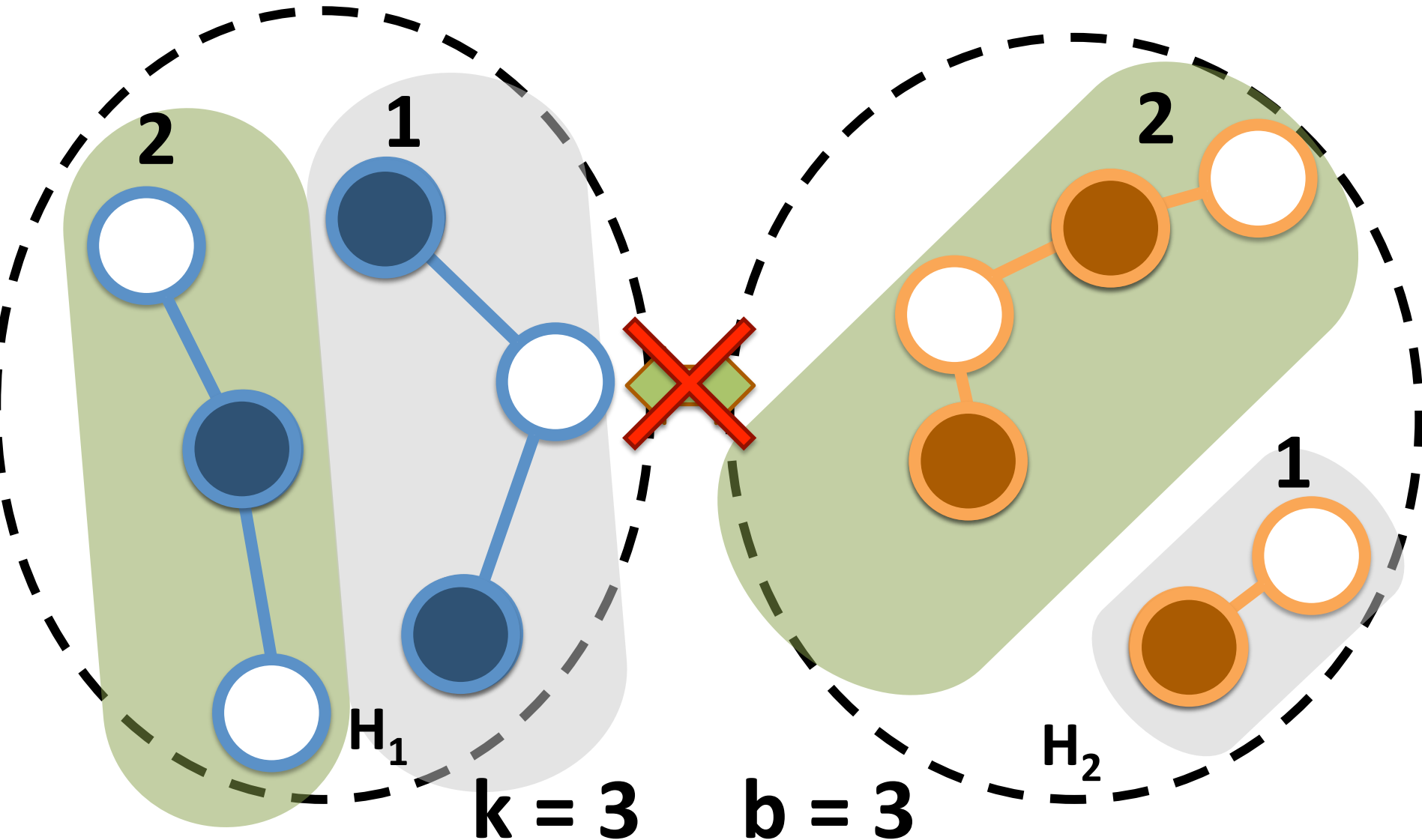


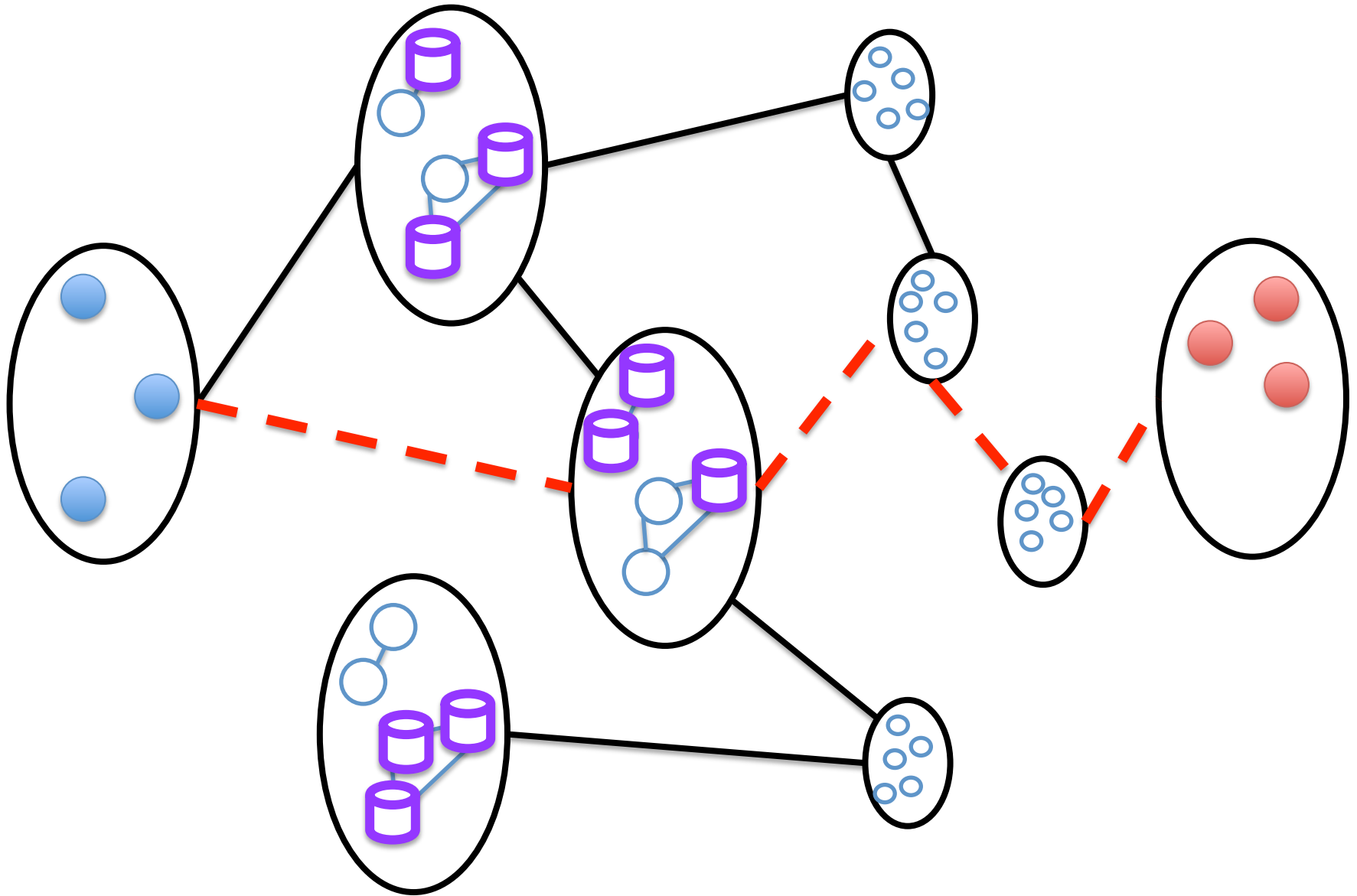


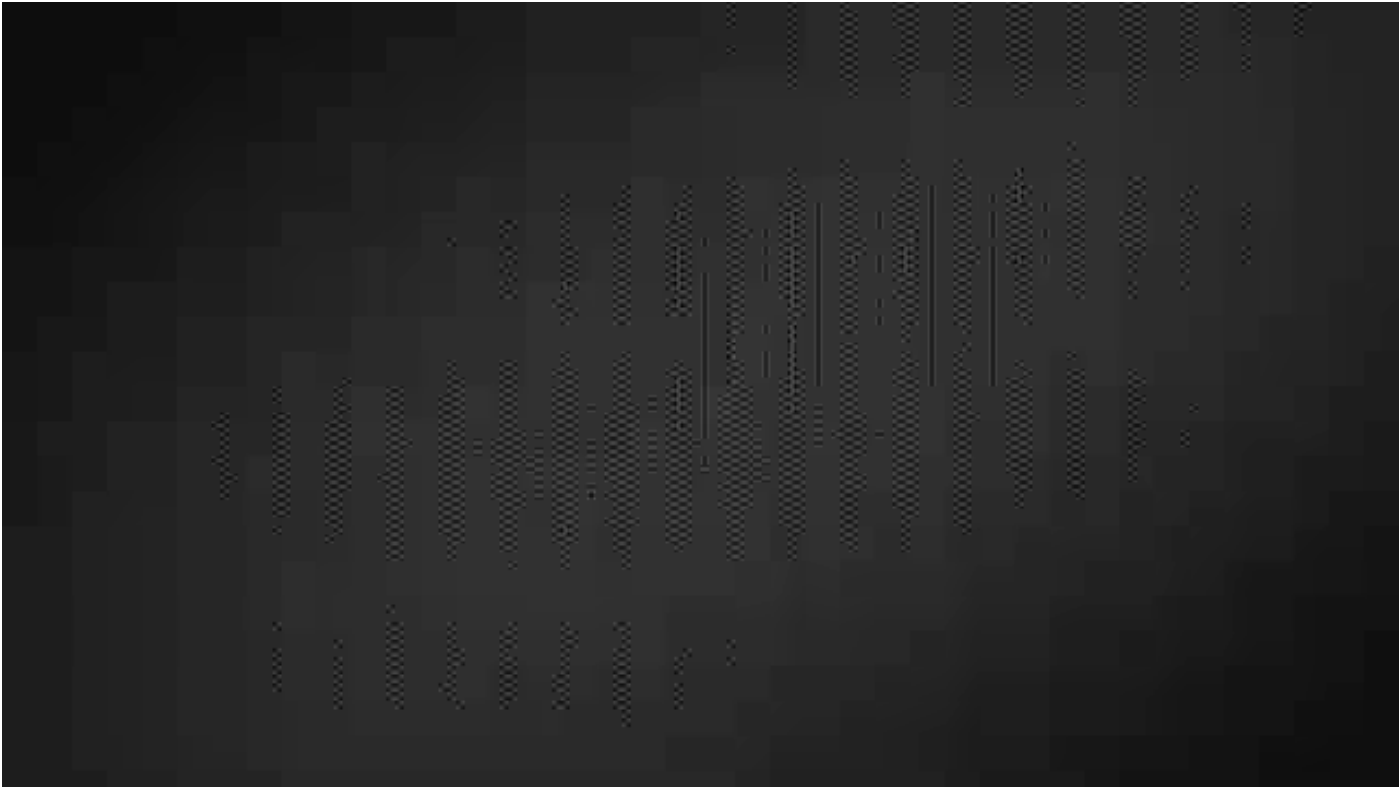
- Objects within each connected component can be rearranged, since the edges within an RPG correspond to valid motions.



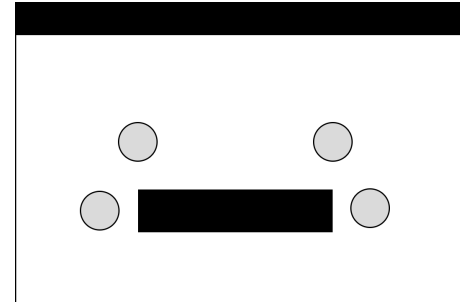
- Hyper nodes that will fail to connect because of the signatures.



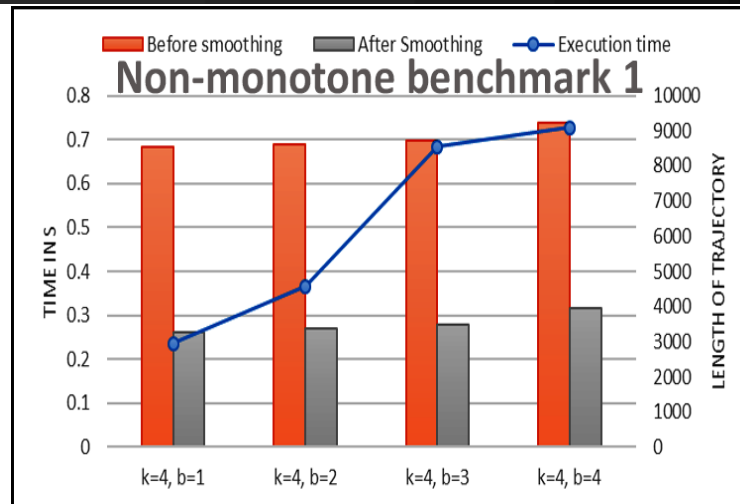
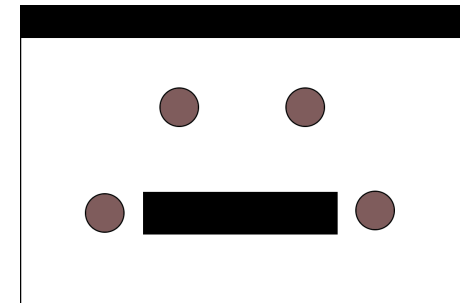


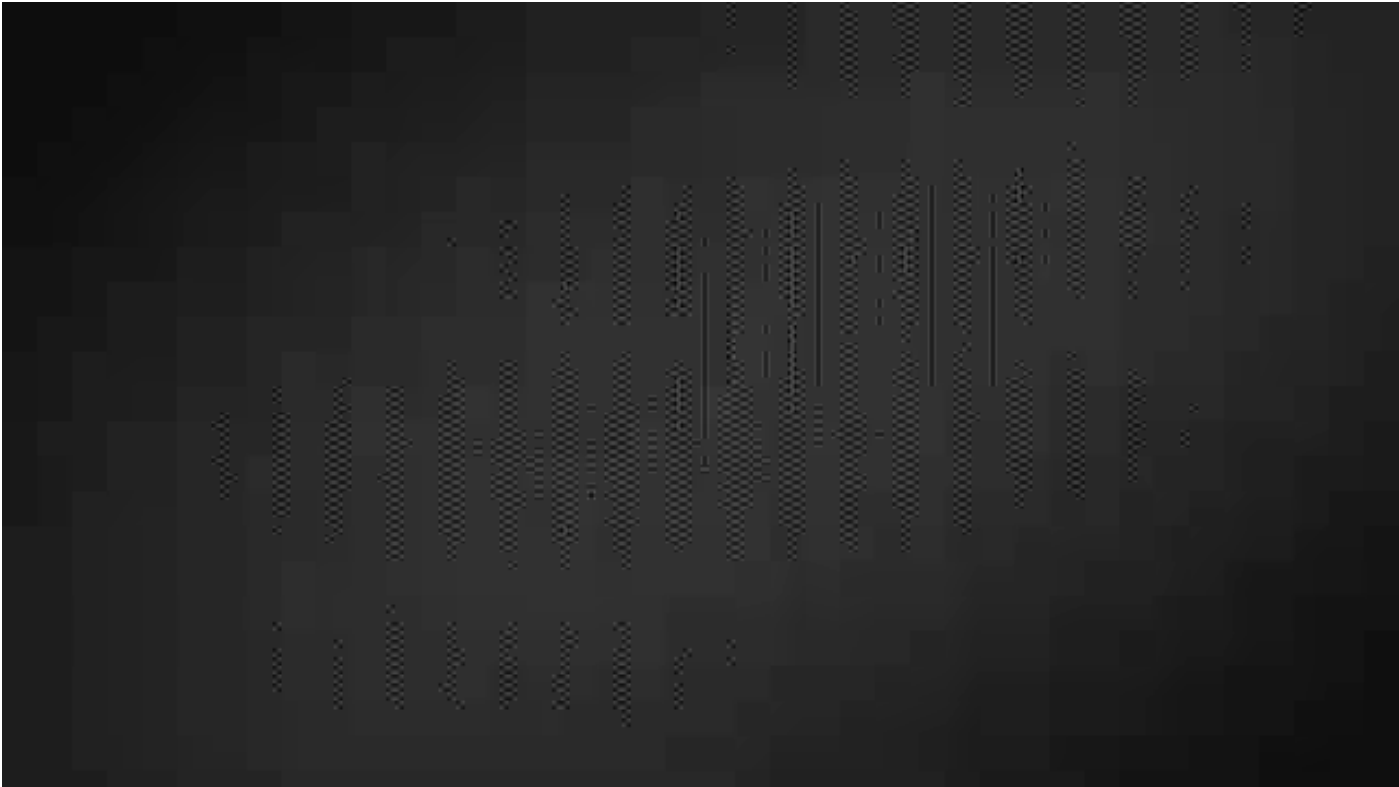


Start

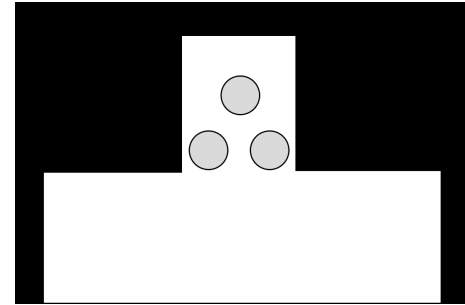


Goal

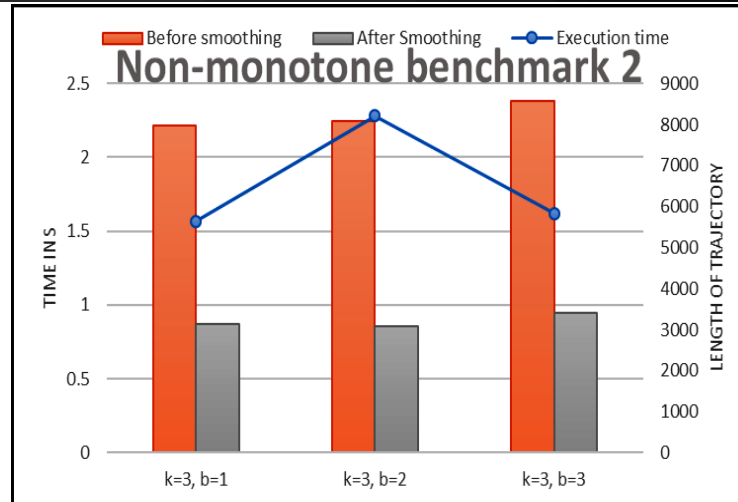
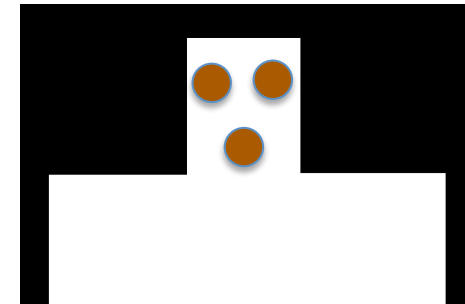




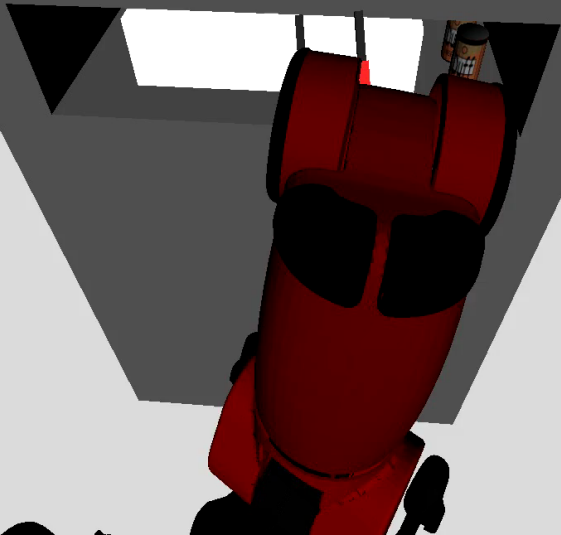
Start



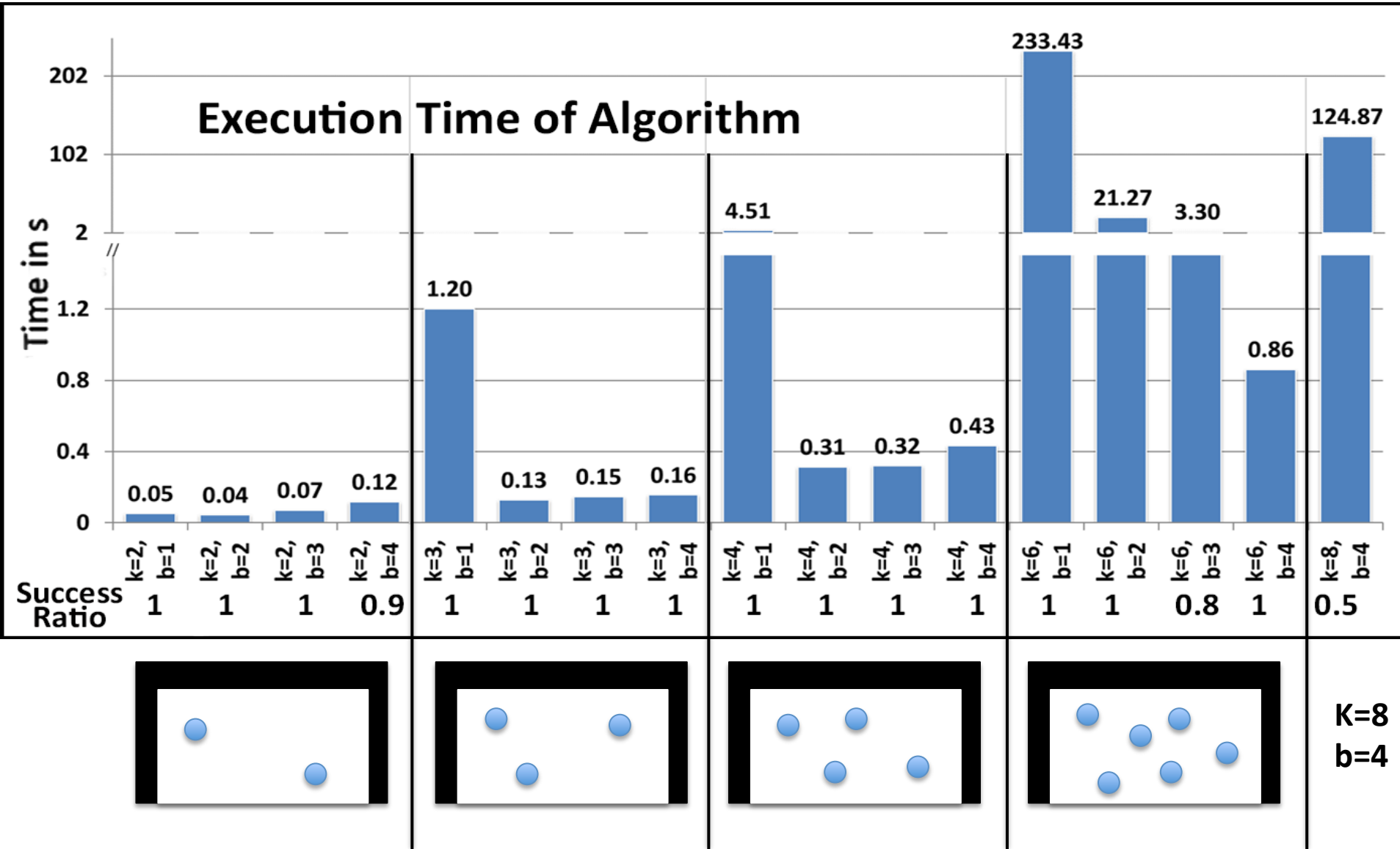
Goal



# From Simulation to Baxter

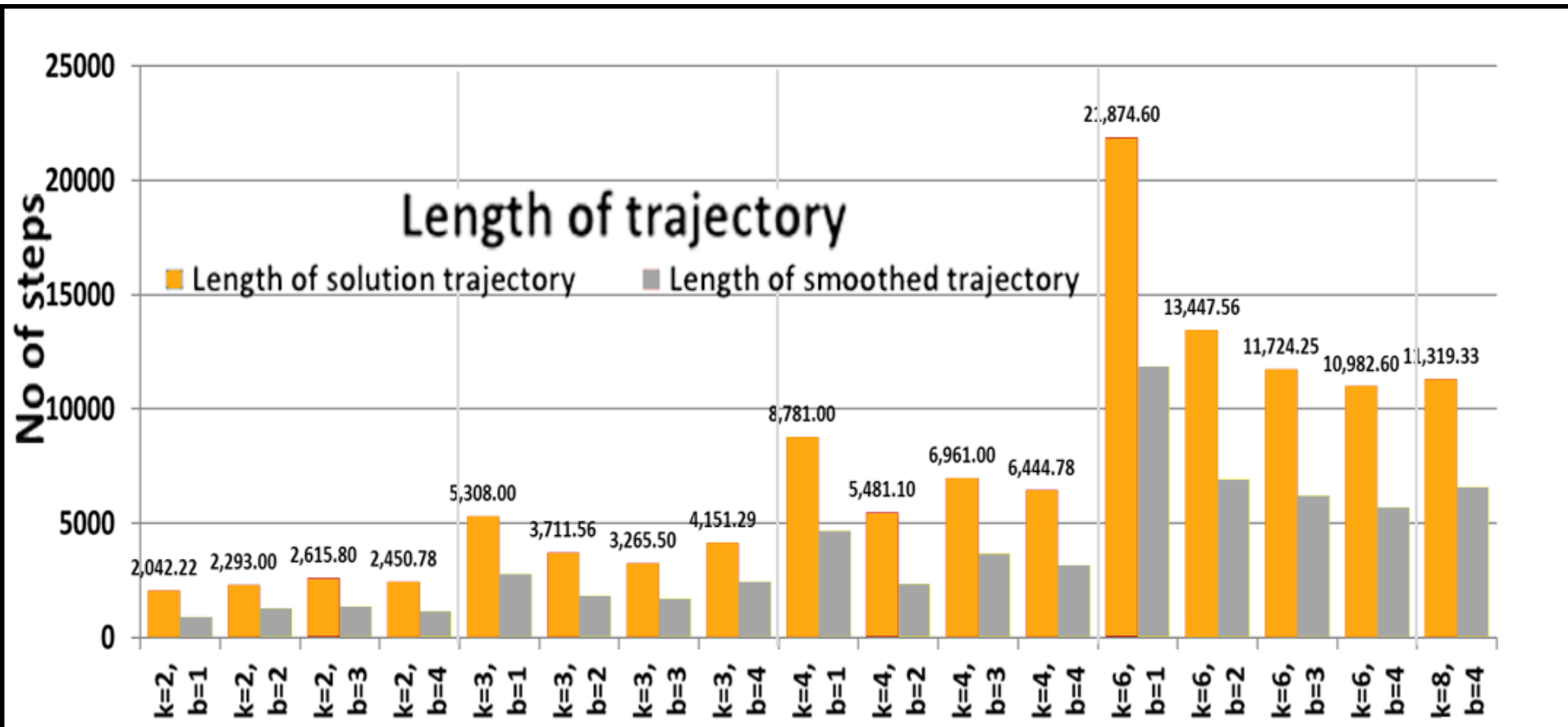


- Randomized placement of poses





- Smaller values of  $b$  reduces the exploration rate, which results in longer trajectories.
- Smoothing shortens, on average, the trajectory by 48%



## Summary:

- Given a precomputed manipulation graph for a single object
  - We can solve rearrangement problems using RPGs in seconds
- Probabilistic completeness can be argued for a class of instances
  - We must be able to retract the arm to the safe configuration

## Future steps:

- Labeled case: Objects with different geometries/labels
- Consider ways to increase connectivity of super-graph
- Improve path quality
- Allow general grasps and resting poses in implementation
- Dual-arm manipulation



Thank you  
for your  
attention!



---

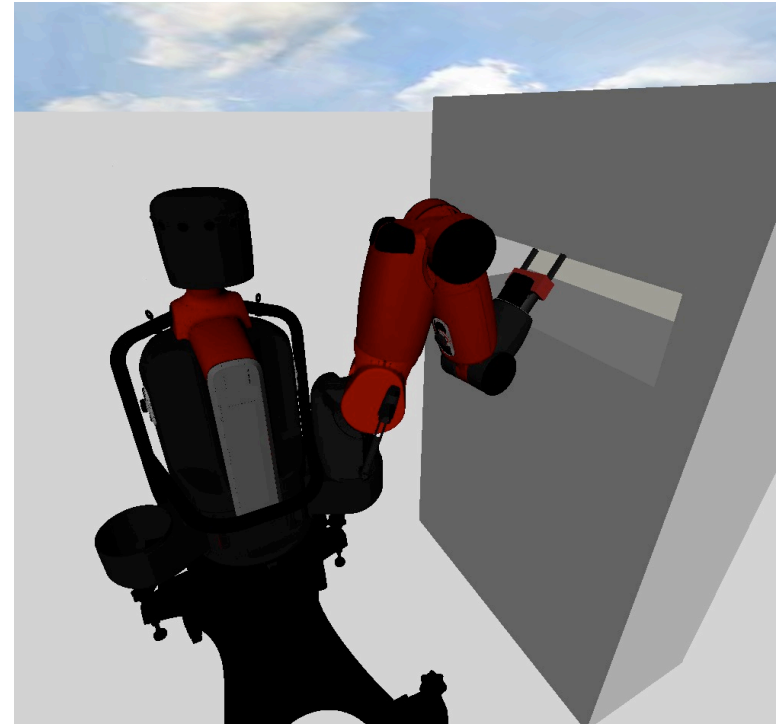
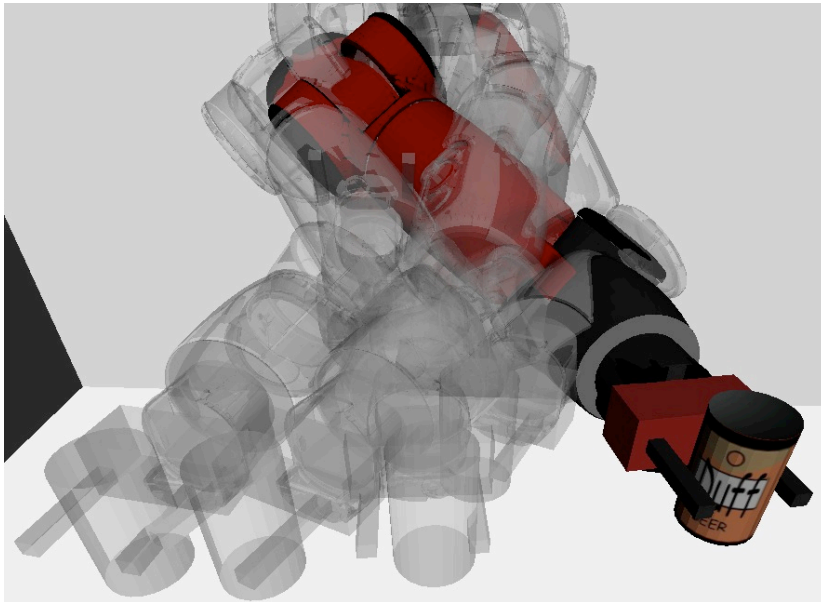
Our research efforts have been supported by:

- the National Science Foundation (NSF),
- the National Aeronautics and Space Administration (NASA),
- the Department of Defense (ONR & DoD TARDEC).

# Backup Slides

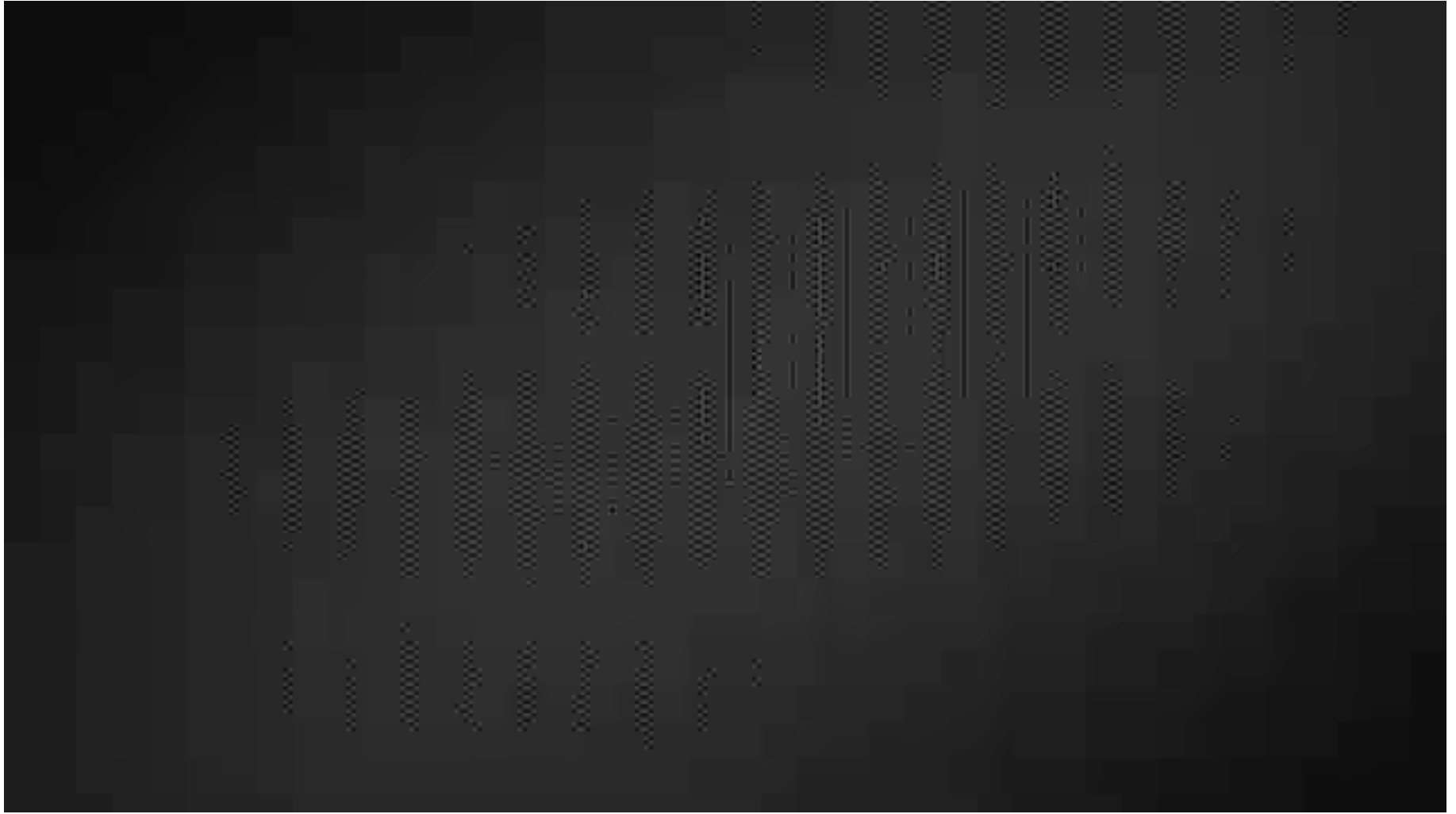
- Safe Arm Configuration.

A collision-free configuration that the arm is safe to return regardless the placement of objects.

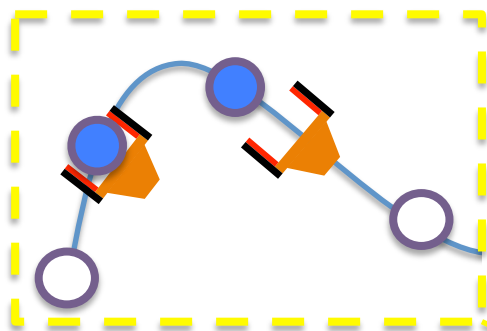


- Stable Object Configuration

A placement of object so they can stay at rest and can be grasped by the robot

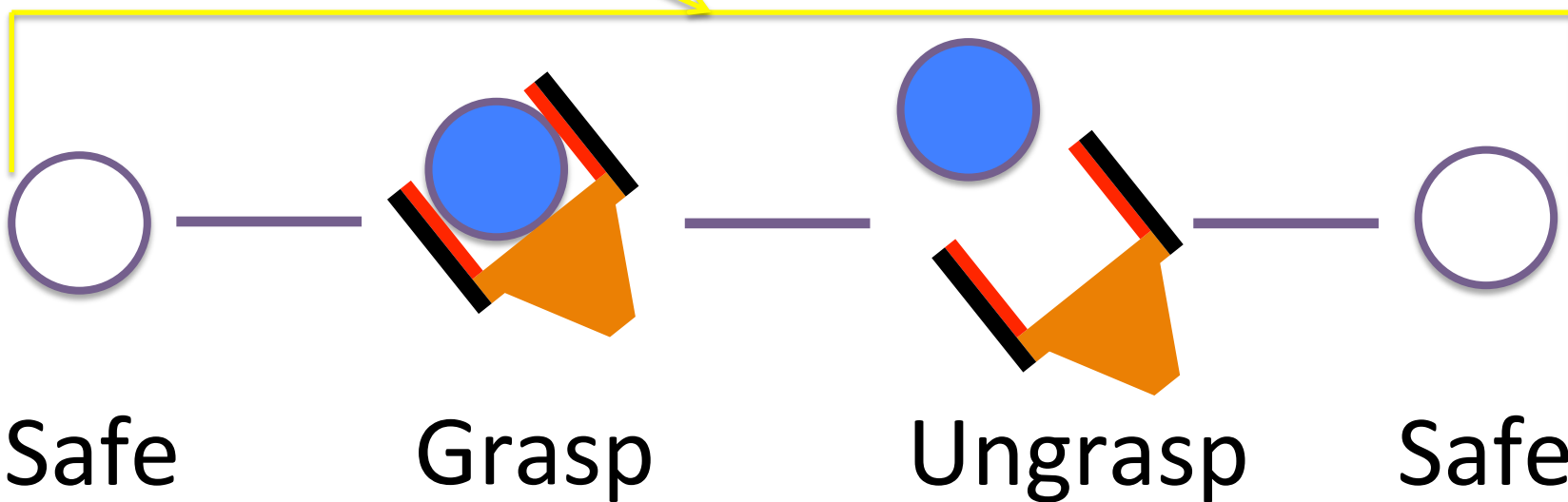


# Smoothing

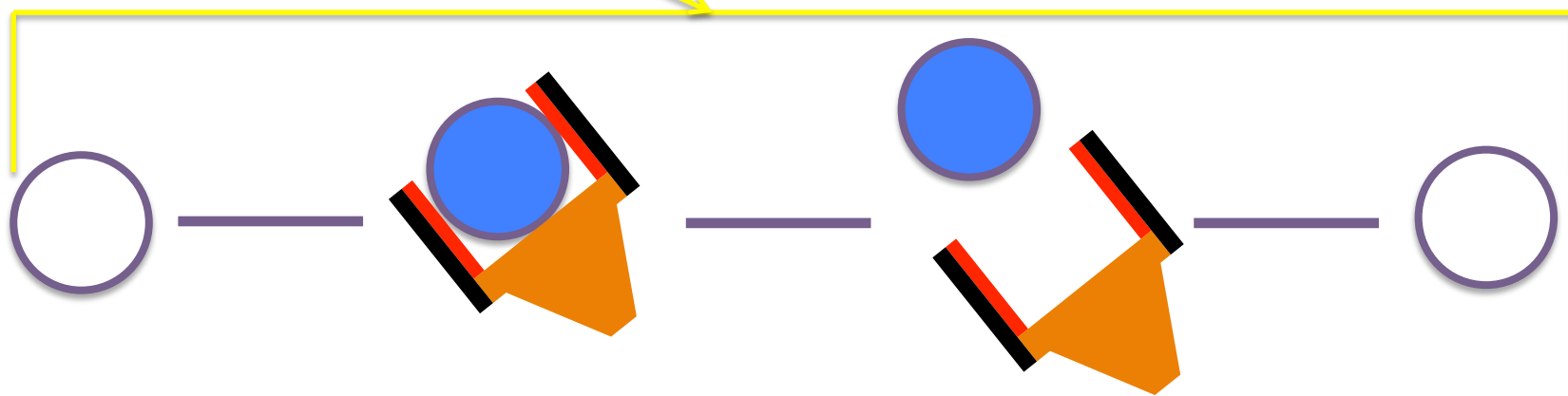
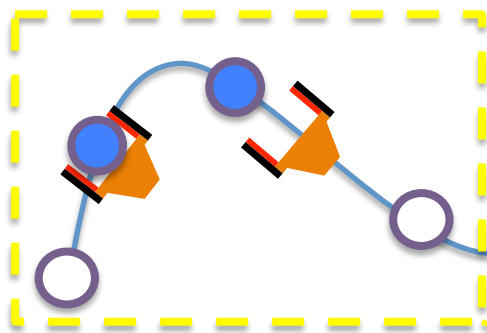


The solution trajectory can be decomposed into 3 separate categories of states

1. Safe State
2. Grasp States
3. Ungrasp States





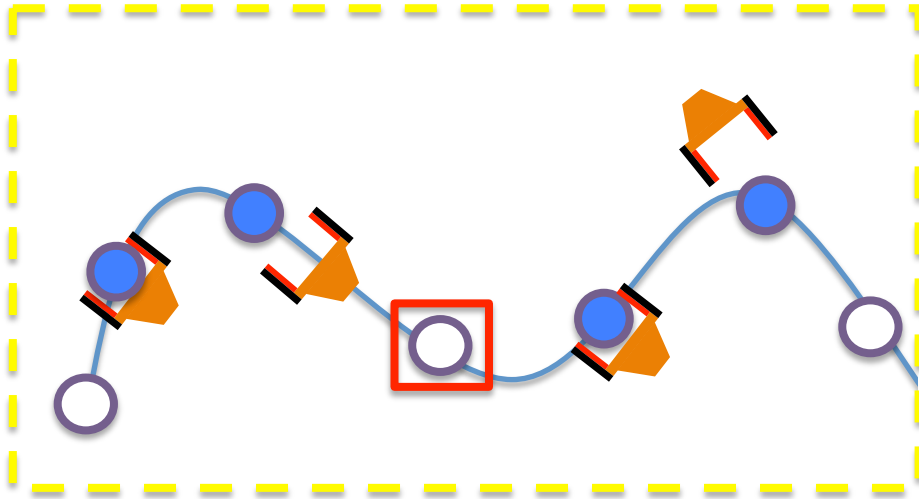


Safe

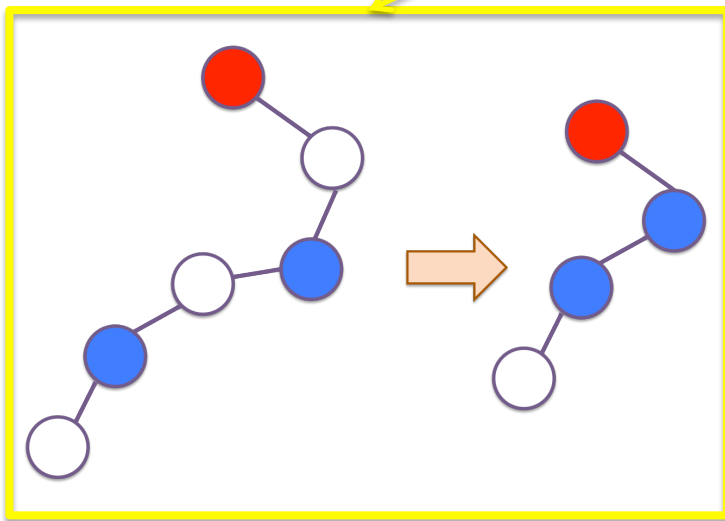
Grasp

Ungrasp

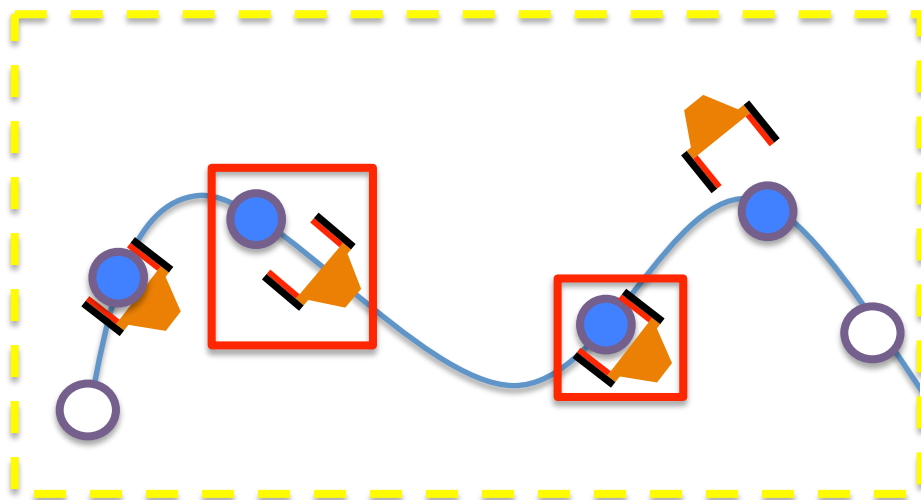
Safe



We identify parts of the trajectory where the robot grasps the same object consecutively.



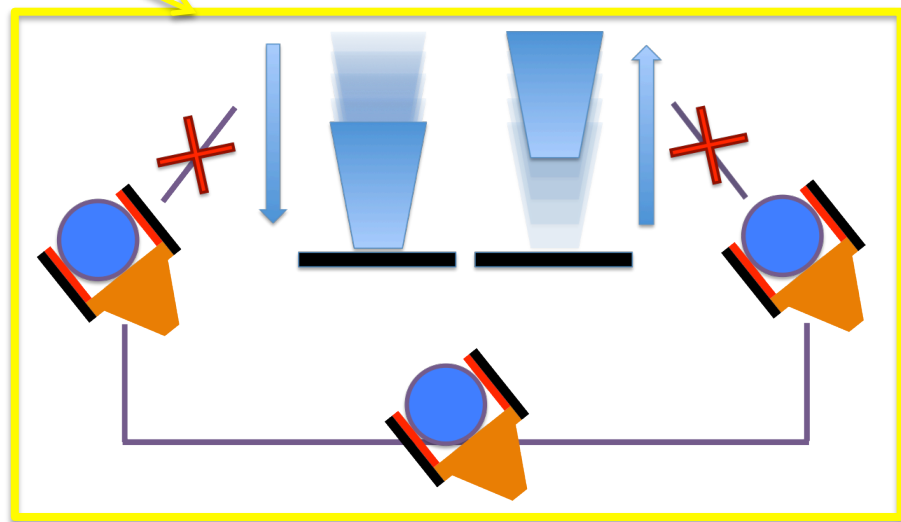
Any intermediate safe states are removed



We identify parts of the trajectory where the robot grasps the same object consecutively.

Next, we identify redundant movements in this sequence.

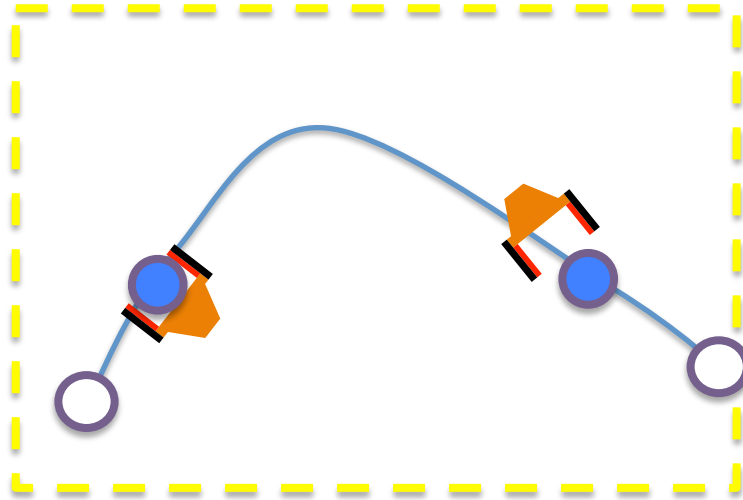
For example, the robot dropping and picking up the same object before moving it again.





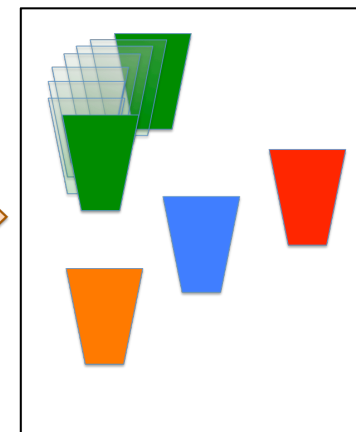
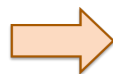
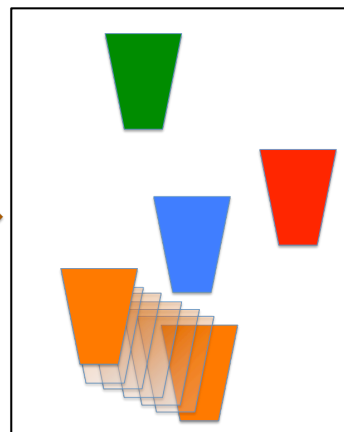
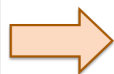
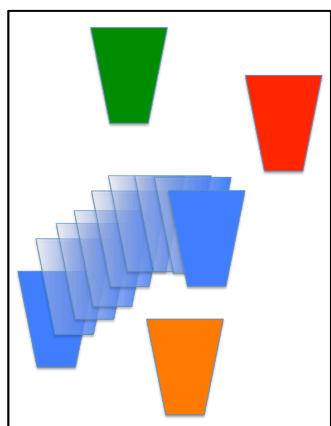
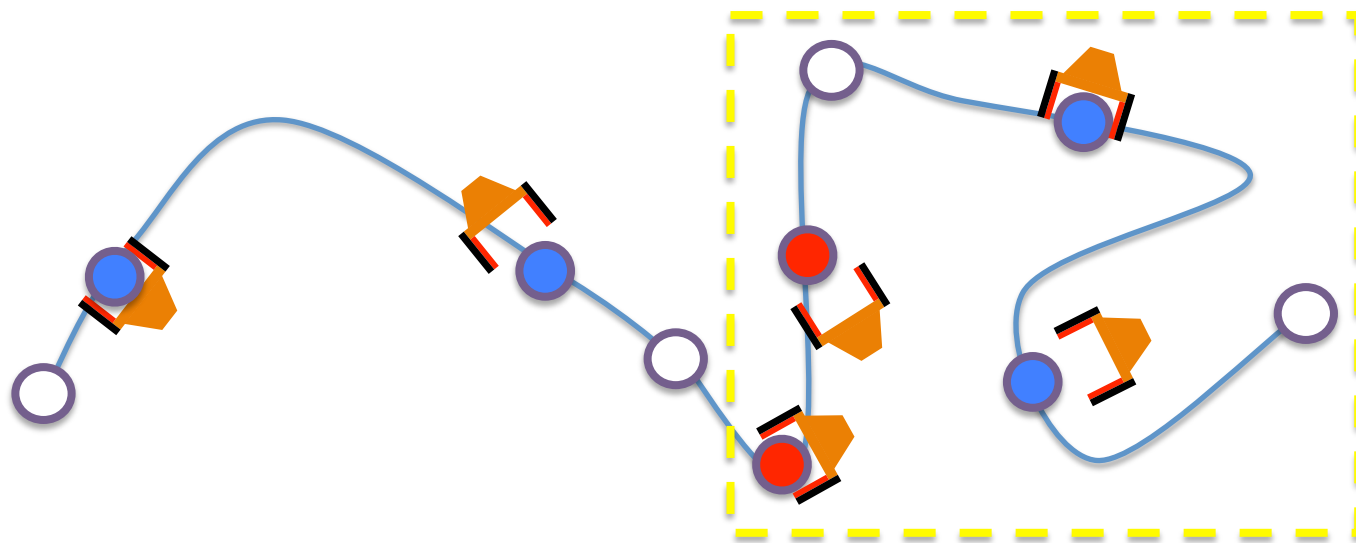
We now can apply standard trajectory smoothing, given a sequence of states from one safe state to another safe state.

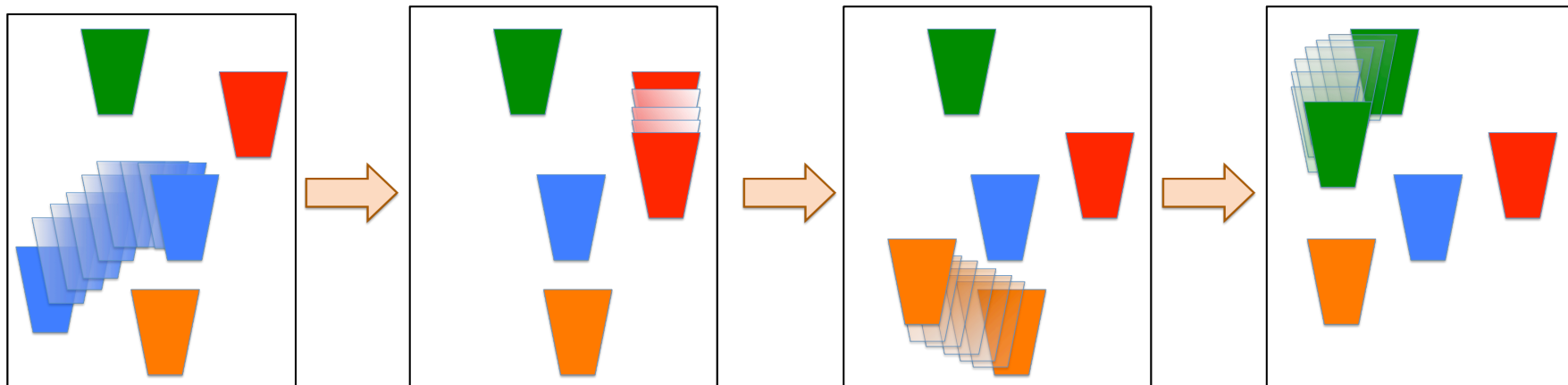
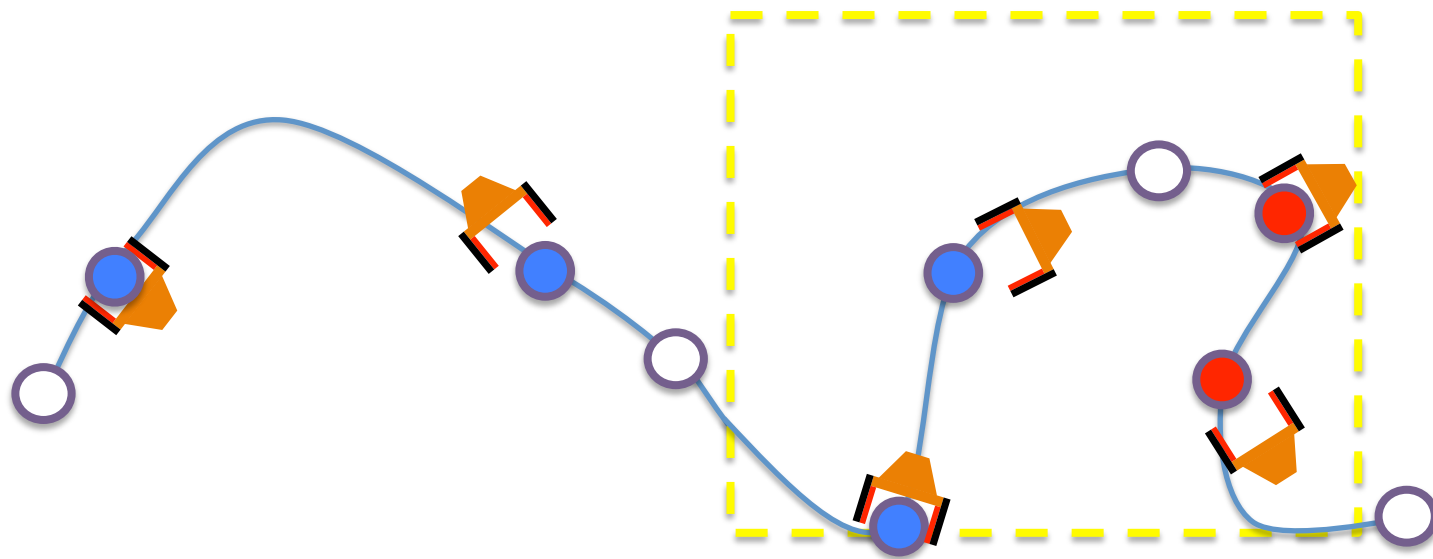
1. Check pairs of states ( $s_1, s_2$ )
2. Compute the shortest trajectory between them
3. If this trajectory is collision free, replace the original trajectory with this new one.

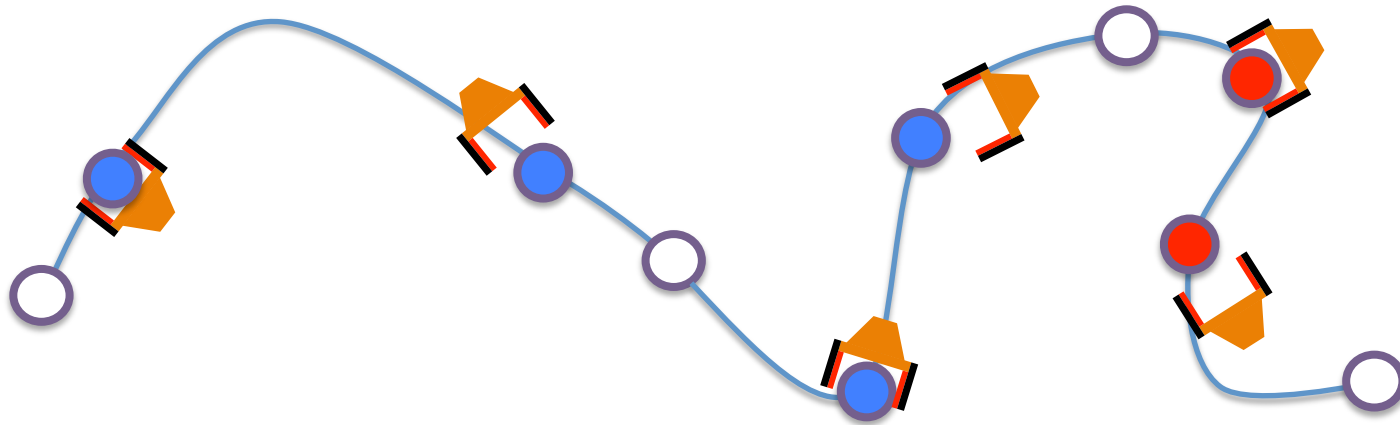


We now can apply standard trajectory smoothing, given a sequence of states from one safe state to another safe state.

1. Check pairs of states ( $s_1, s_2$ )
2. Compute the shortest trajectory between them
3. If this trajectory is collision free, replace the original trajectory with this new one.







- Individual phases, such as the standard smoothing, can be applied.
- Or, the entire smoothing process could also be repeated.
- This has the potential of yielding a new, shorter solution.
- In practice, one iteration of the smoothing process will provide the largest reduction in the solution trajectory.



WITHOUT SMOOTHING

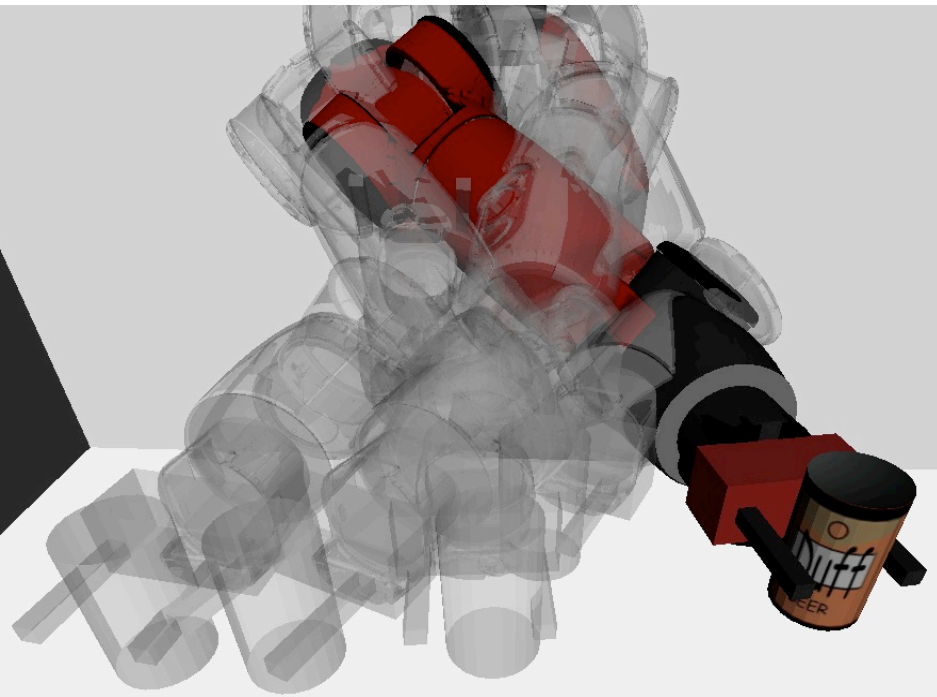


VS

WITH SMOOTHING

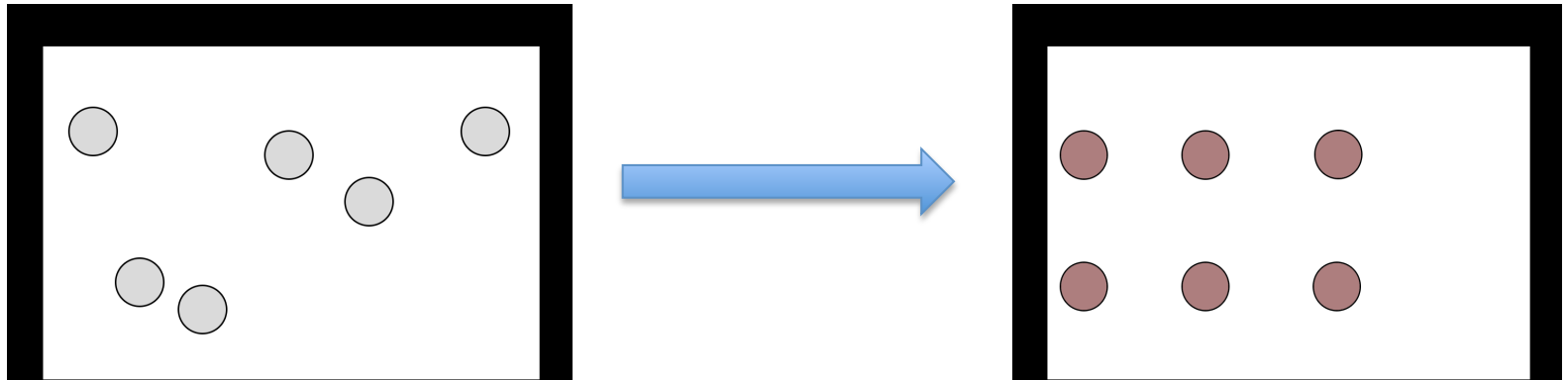


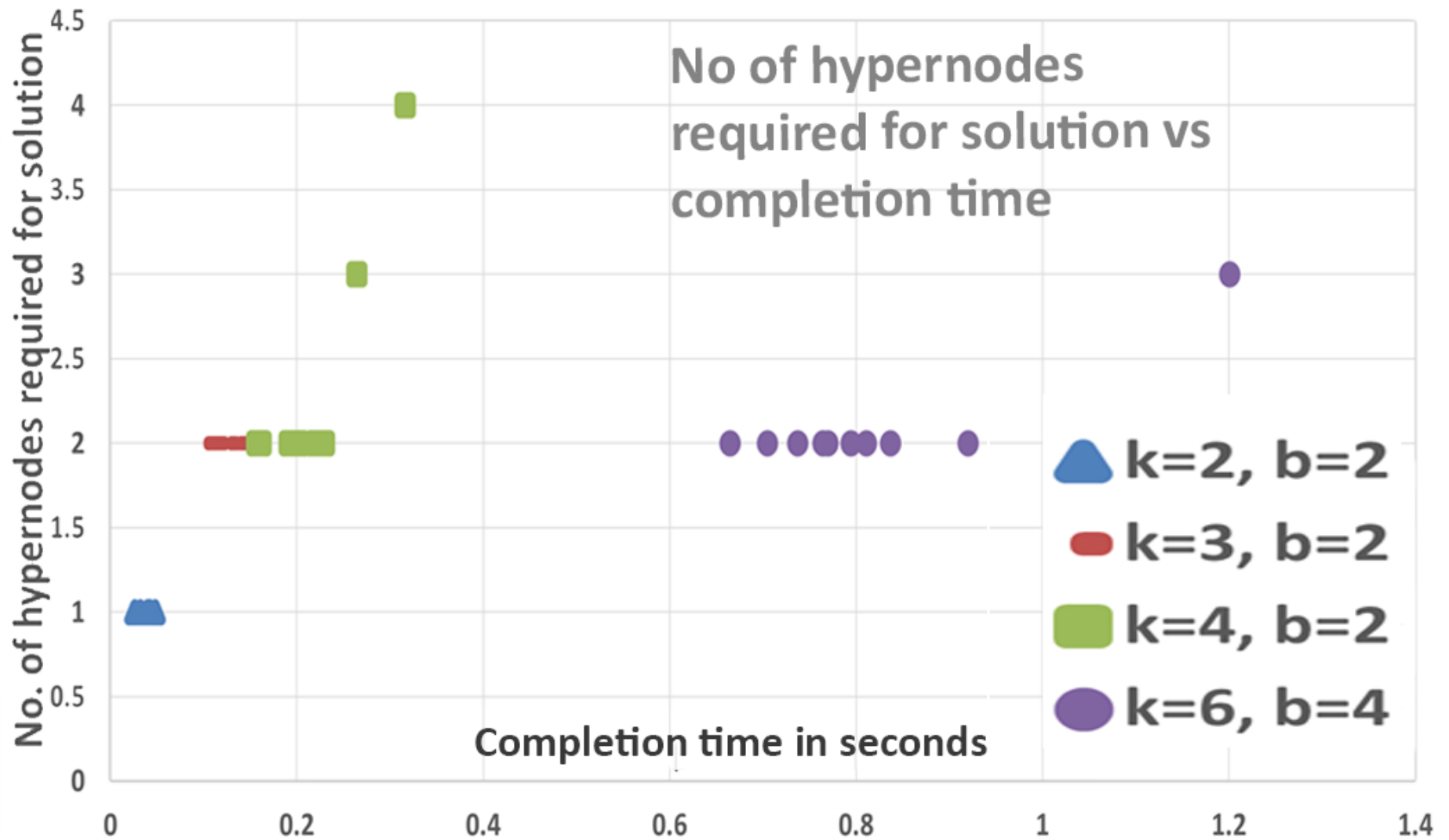
- The experiments were conducted both in simulation and on a Baxter robot (7 DOF).



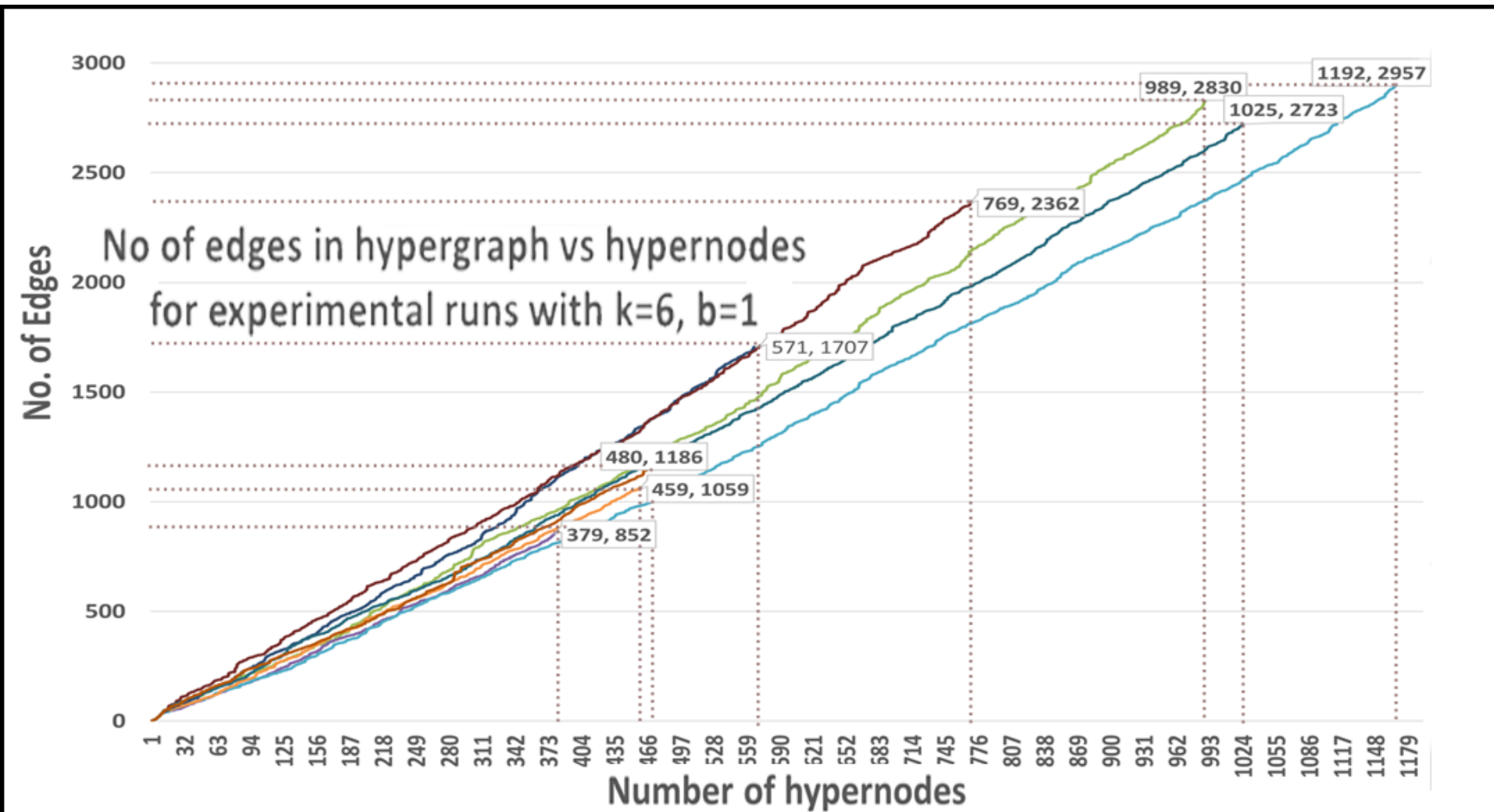
- We evaluate the scalability of the approach, and also showcase its ability to solve non-monotone problems.

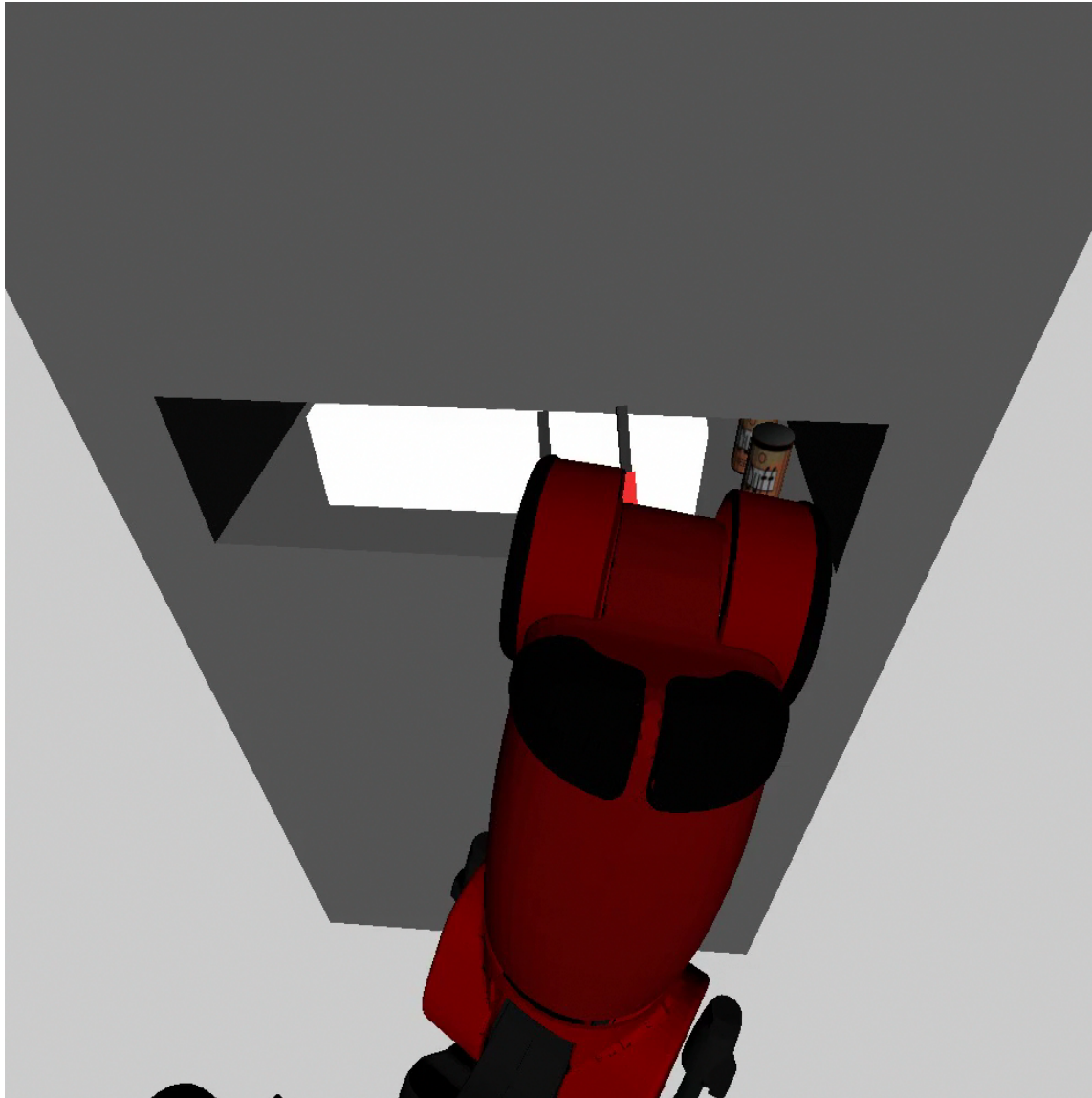
- Here are the metrics we measured...
  - 1. Execution Time:** How fast were we able to solve the problem, and with what success rate?
  - 2. Solution Quality:** How short were the trajectories?
  - 3. Connectivity:** How many edges connect our hypernodes?





- Randomized placement of nodes





Thank you!



<http://www.pracsyslab.org>